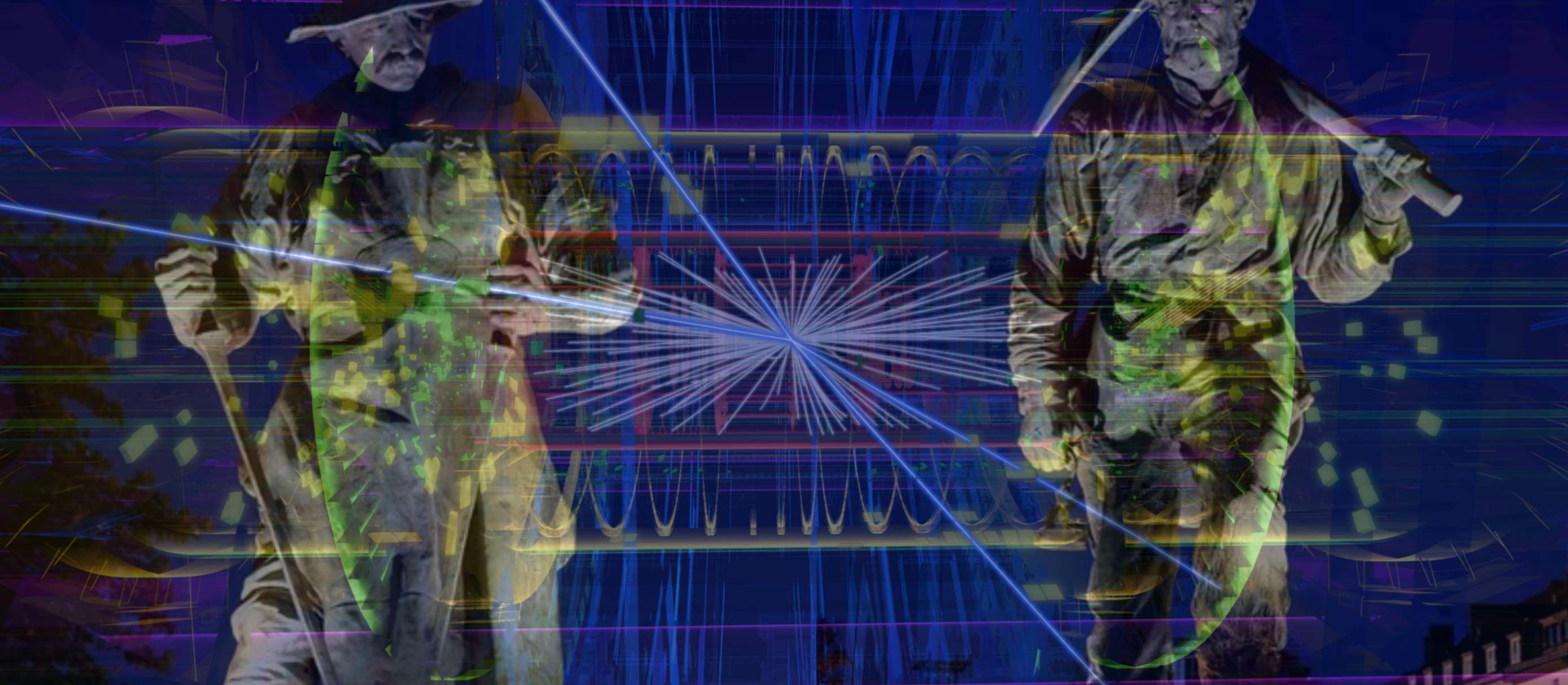




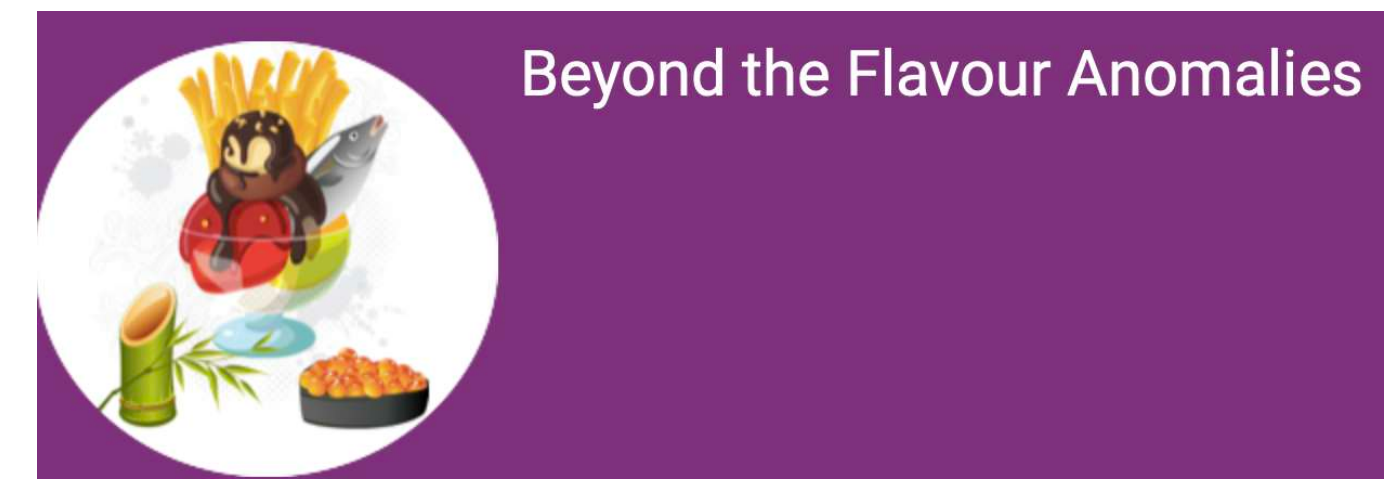
The Outlook for Hadronic Calculations



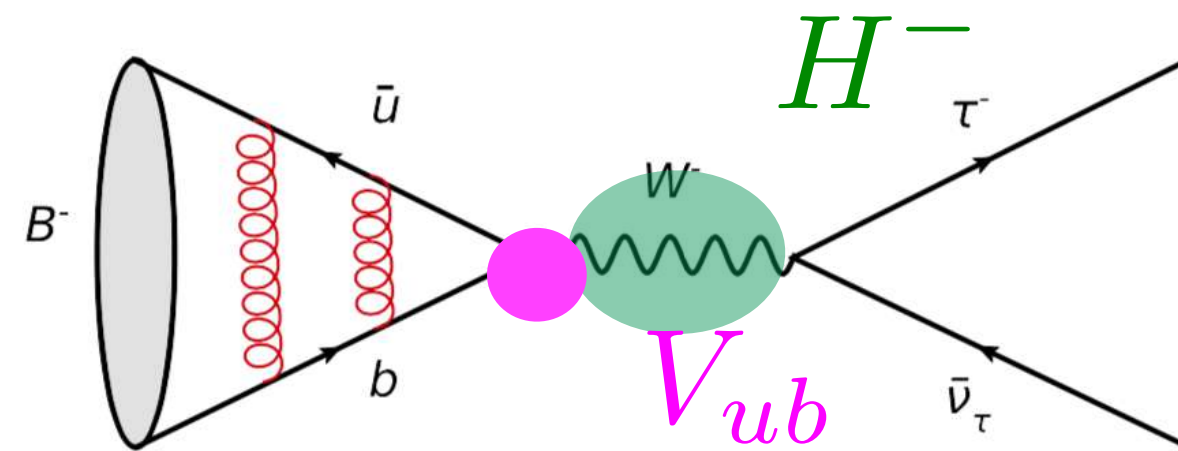
Beyond the Flavour Anomalies

28.4.2022
Alexander Lenz

Hadronic difficulty of Meson Decays



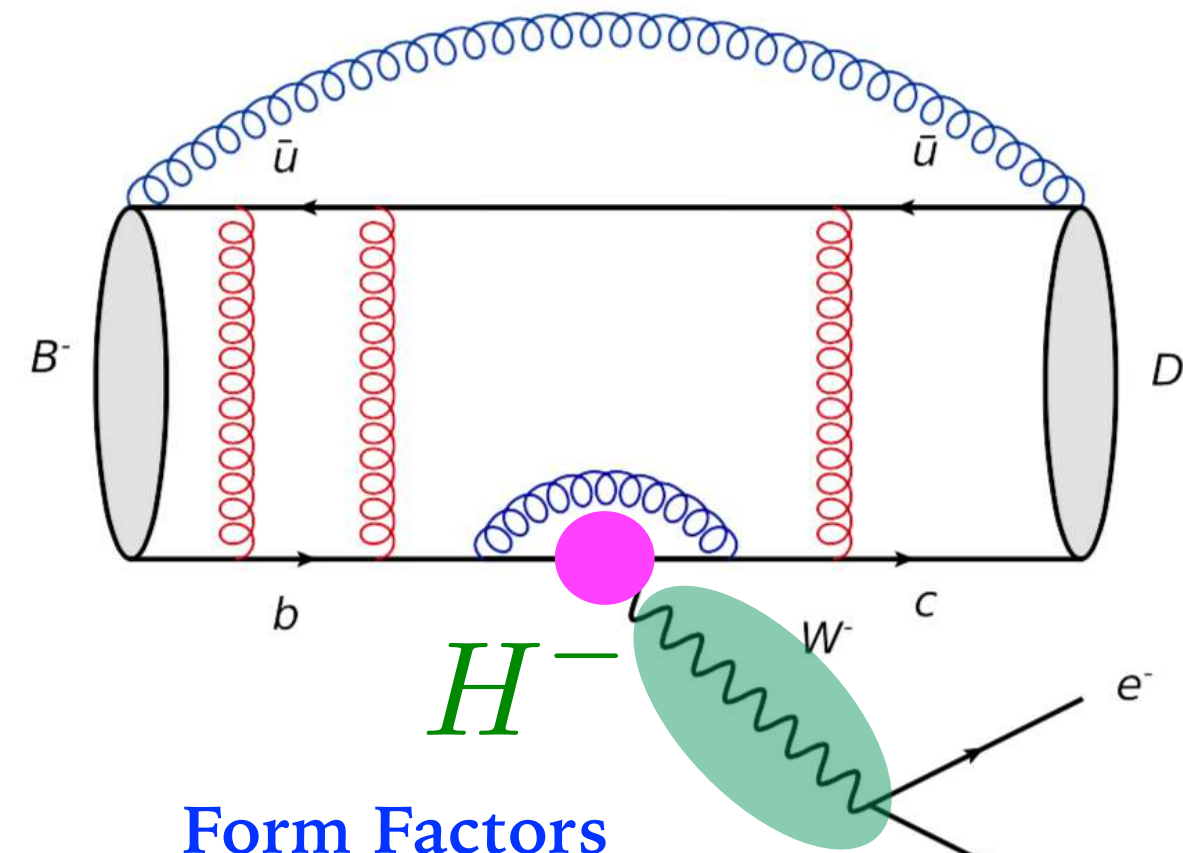
• Leptonic Decays



Decay constant

$$\langle 0 | \bar{b} \gamma^\mu \gamma_5 u | B_q(p) \rangle = i f_{B_q} p^\mu$$

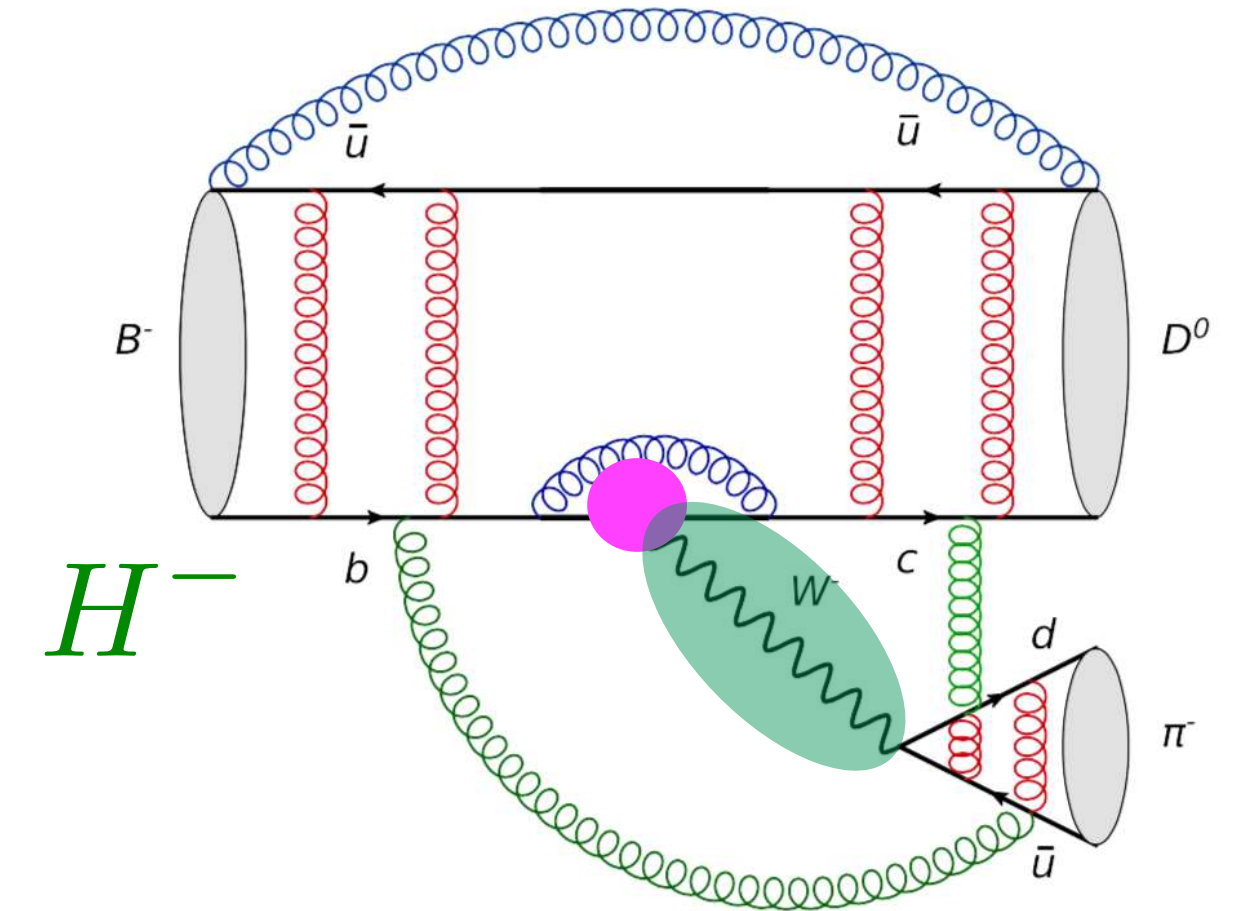
• Semileptonic Decays



Form Factors

$$\langle D^0(p_D) | \bar{c} \gamma_\mu b | B^-(p_B) \rangle = f_+^{B^- \rightarrow D^0}(q^2) \left(p_B^\mu + p_D^\mu - \frac{m_B^2 - m_D^2}{q^2} q^\mu \right)$$

• Non-leptonic Decays



Factorisation

$$\langle D^0 \pi^- | \bar{c} \gamma_\mu (1 - \gamma_5) b \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d | B^- \rangle$$

$$\approx \langle D^0 | \bar{c} \gamma_\mu (1 - \gamma_5) b | B^- \rangle \cdot \langle \pi^- | \bar{u} \gamma^\mu (1 - \gamma_5) d | 0 \rangle$$

I) Imaginary part of CKM-elements = CP Violation

II) Instead of a W-Boson a charged Higgs particle could be exchanged

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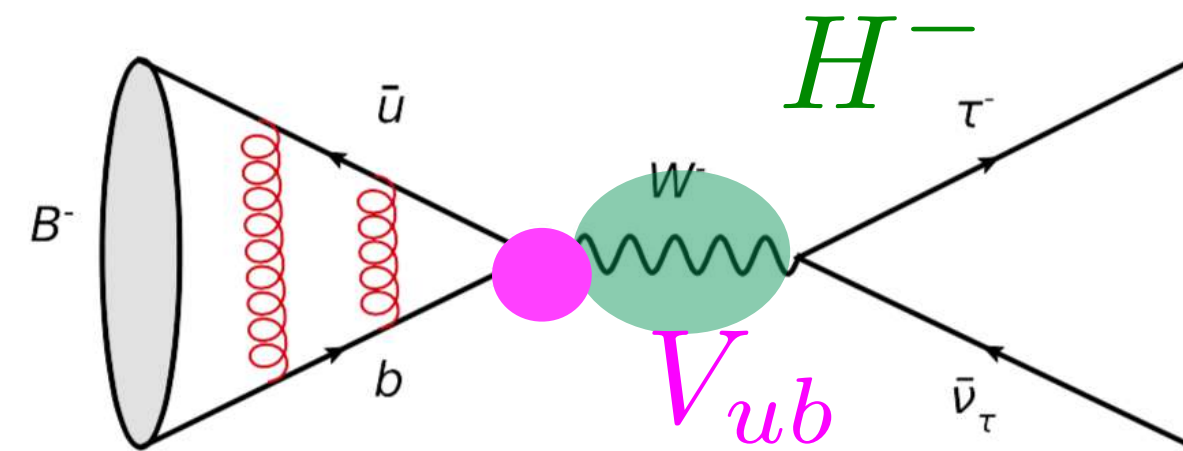
Non-perturbative: decay constants, form factors, factorisation

IV) Determination of SM-Parameter

Hadronic difficulty of Meson Decays



• Leptonic Decays



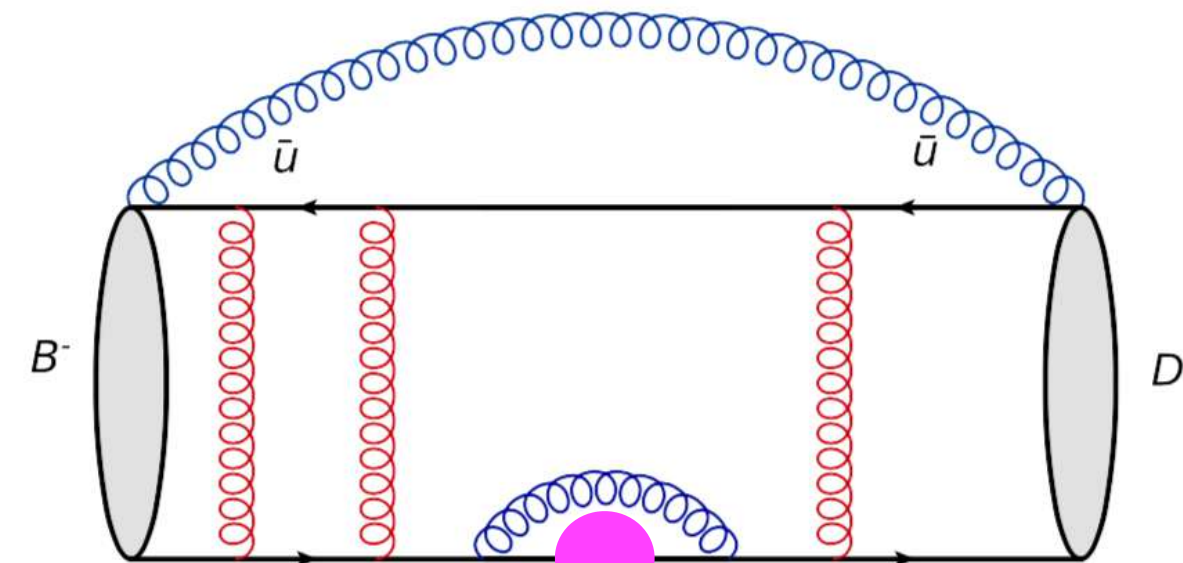
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Ancient B anomalies

Tree: V_{ub}, V_{cb}

• Semileptonic Decays



Form Factors

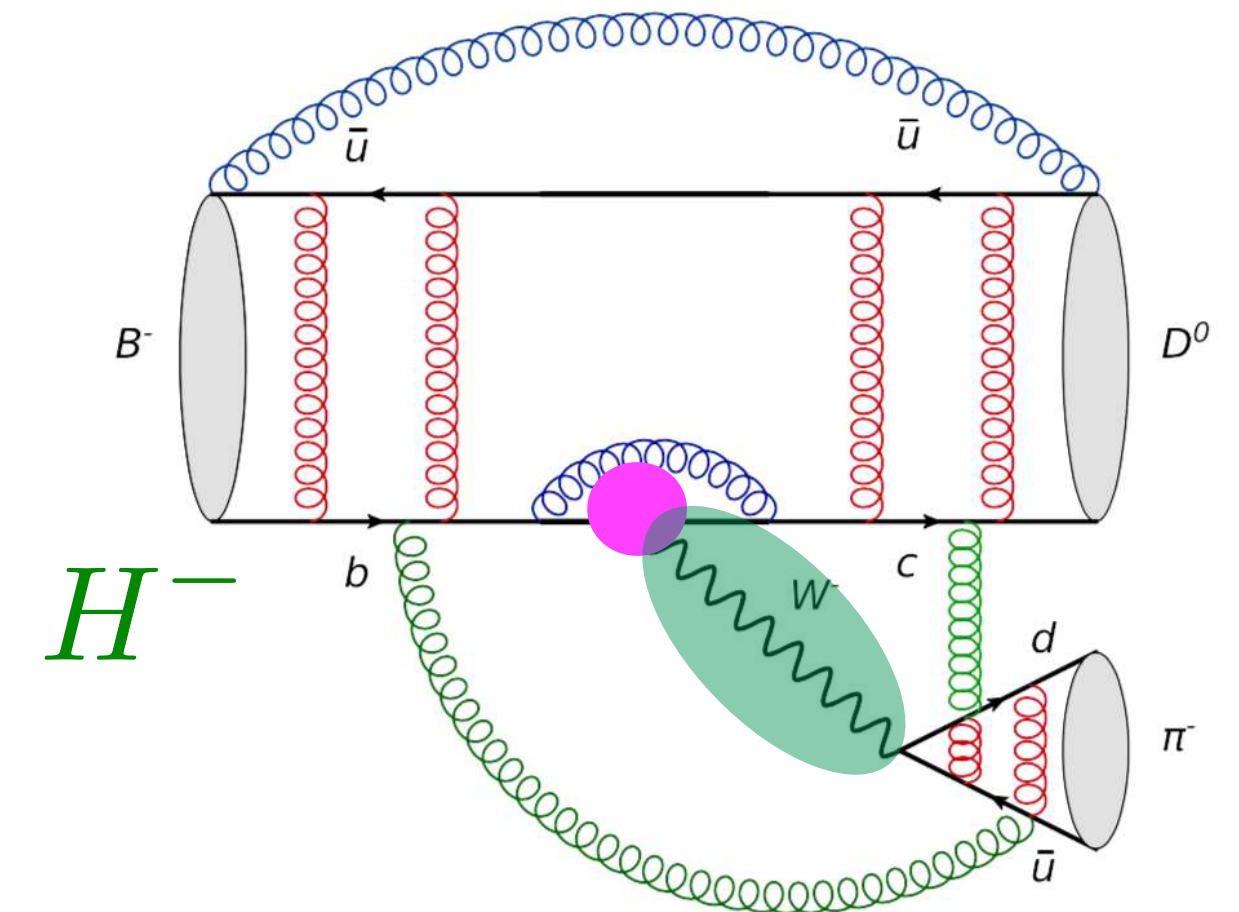
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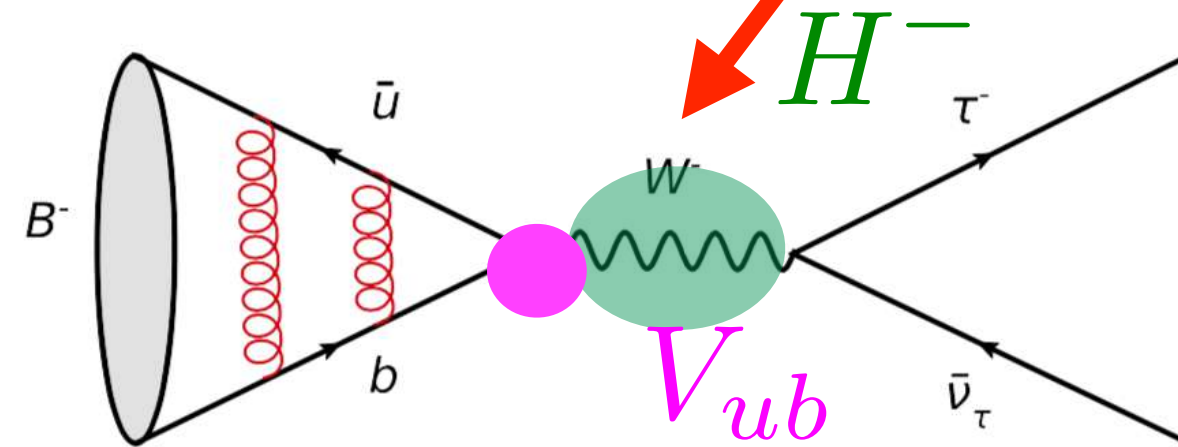
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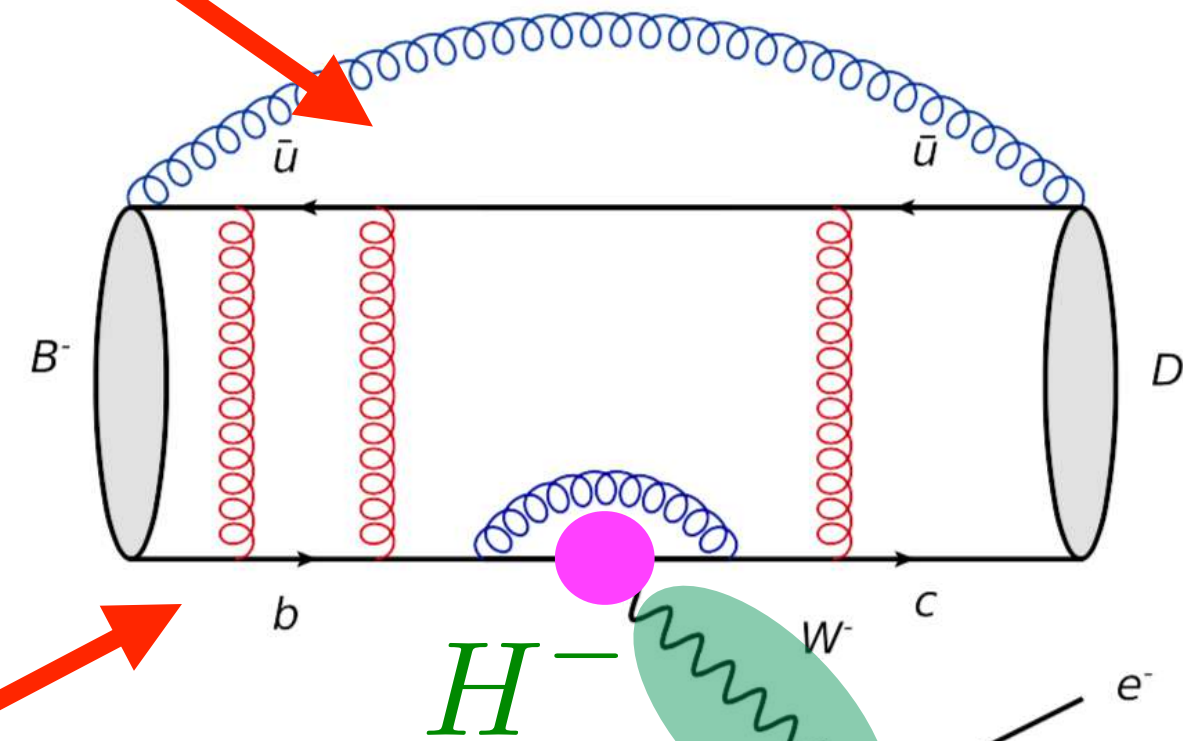
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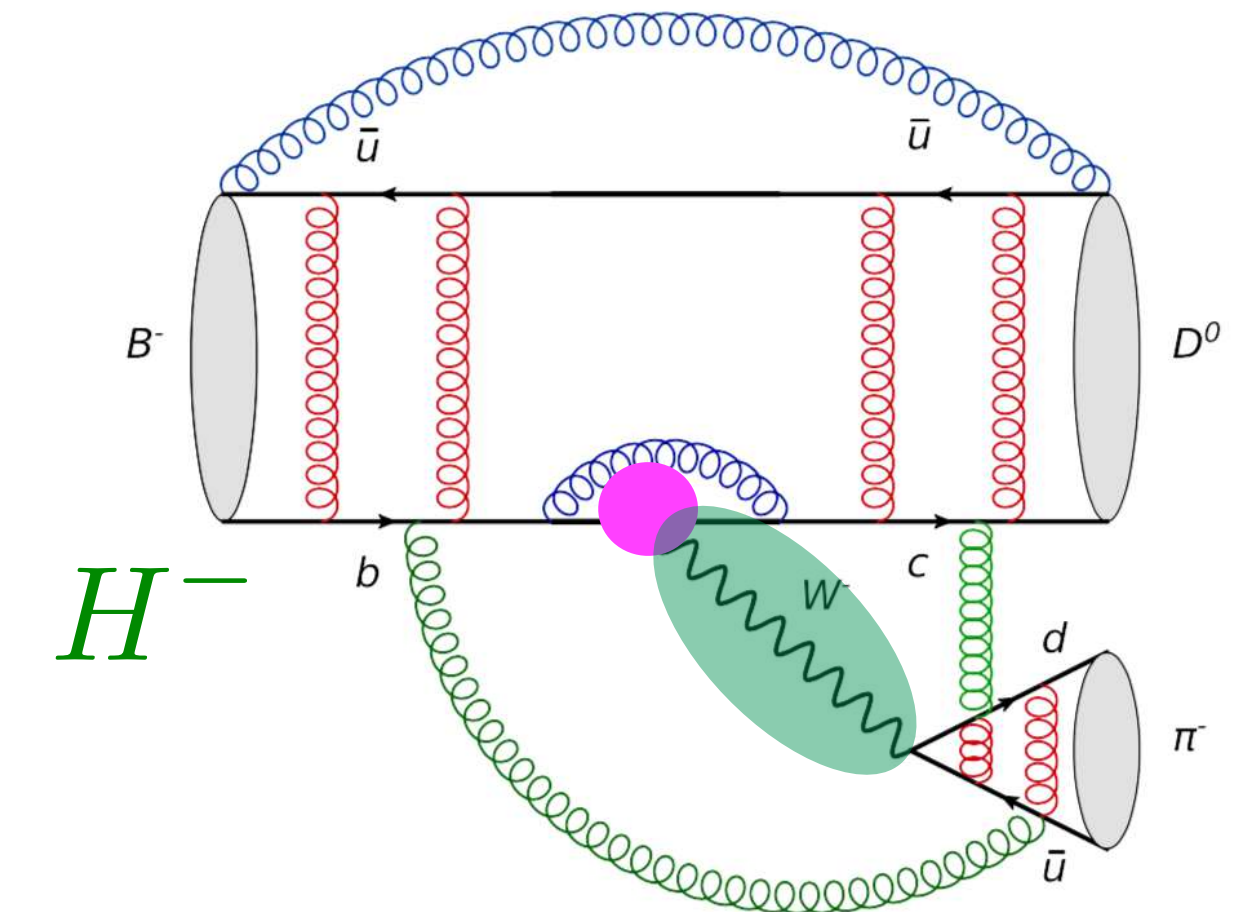
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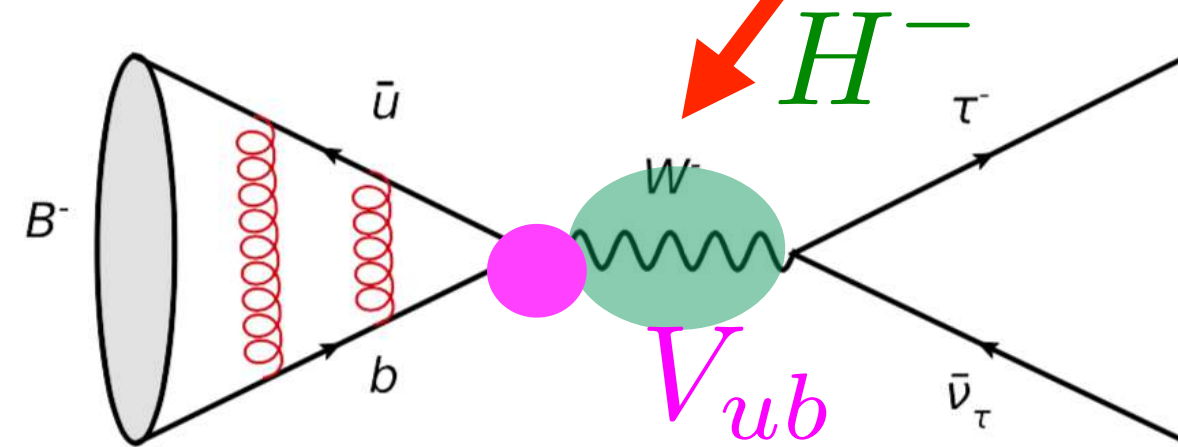
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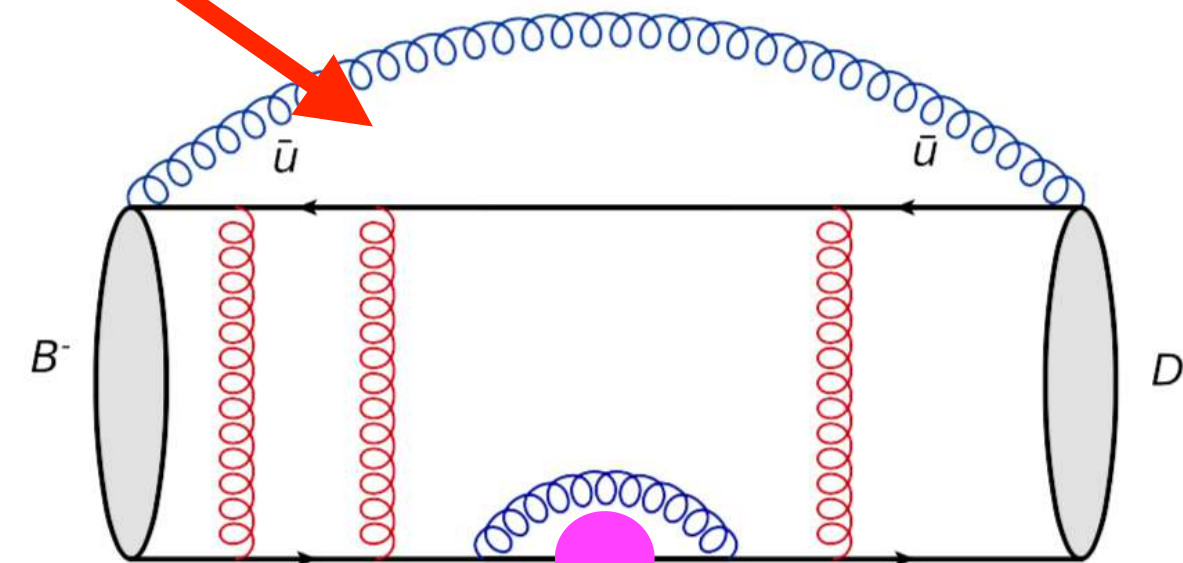


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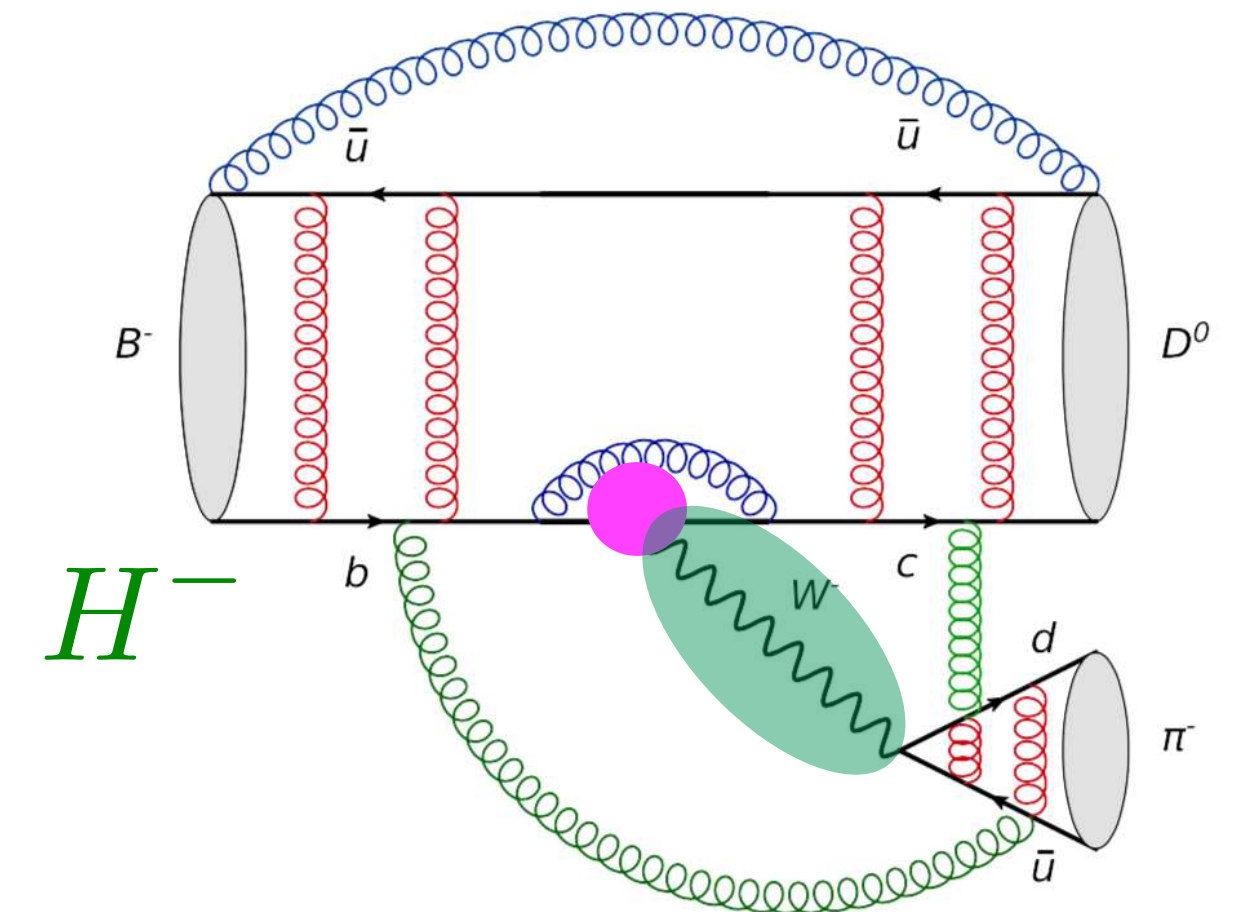


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$b \rightarrow cl\nu$ anomalies
Tree

• Non-leptonic Decays



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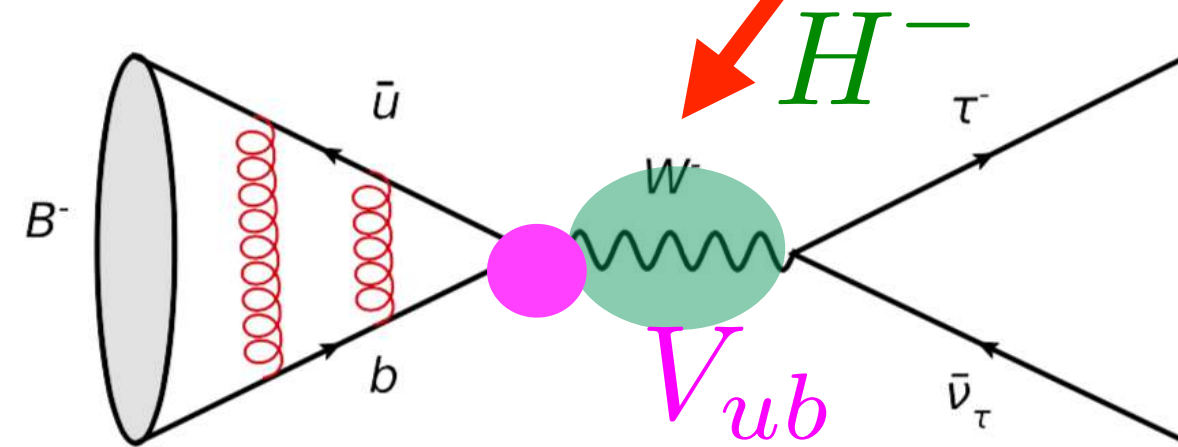
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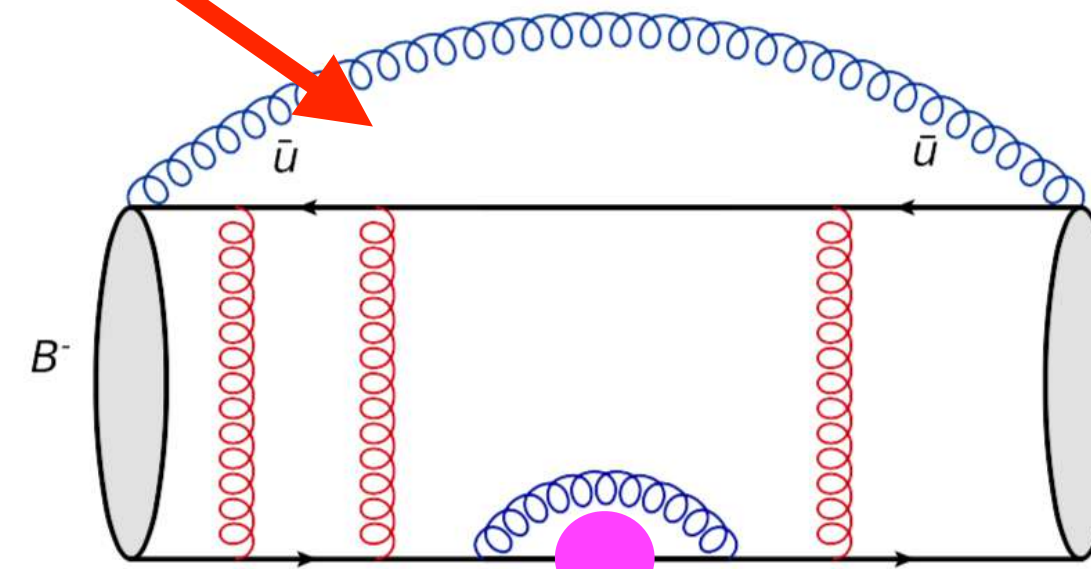
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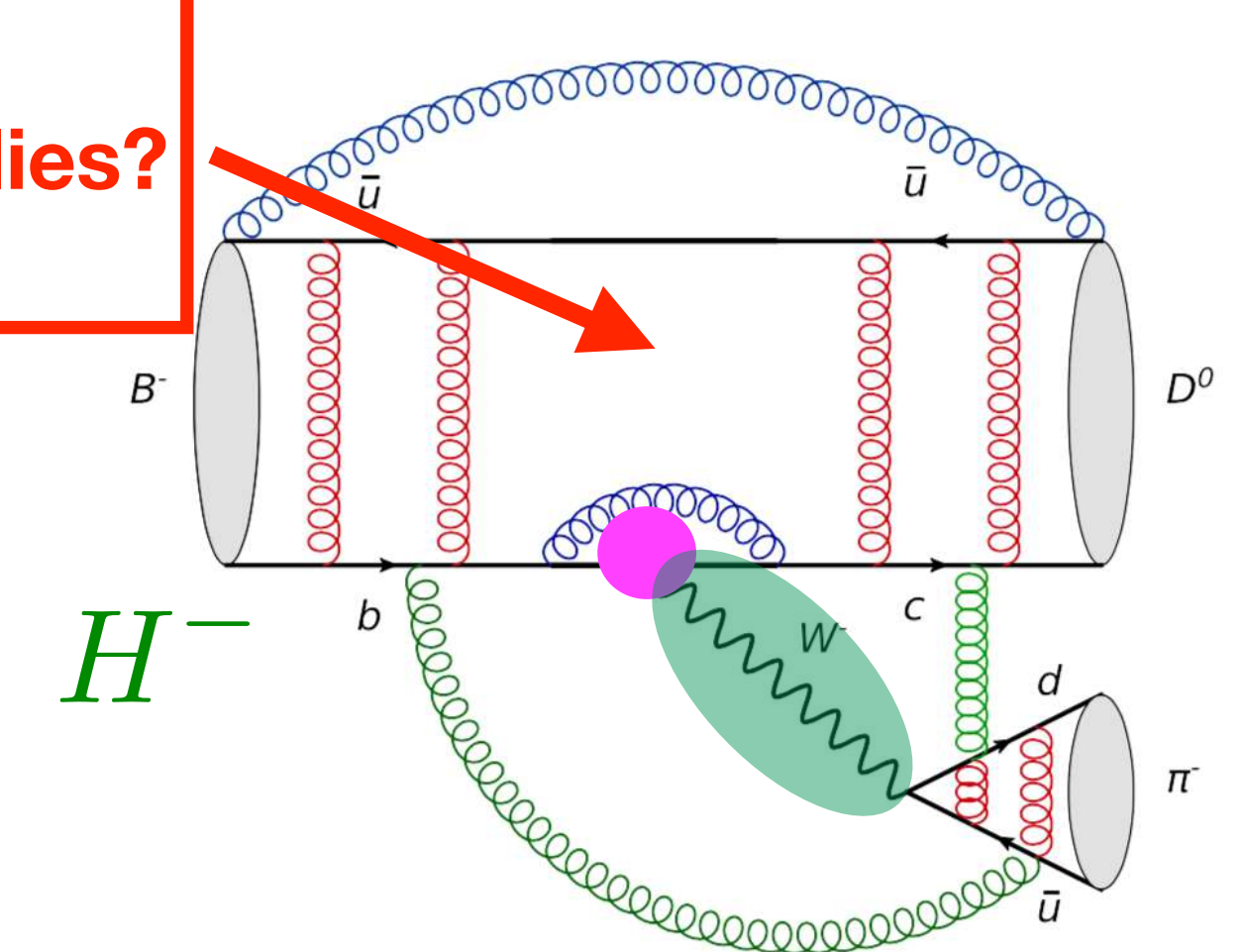


$b \rightarrow sll$ anomalies
Loop

• Semileptonic Decays



• Non-leptonic Decays



New
B anomalies?
Tree

Decay constant

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Tree: V_{ub}, V_{cb}

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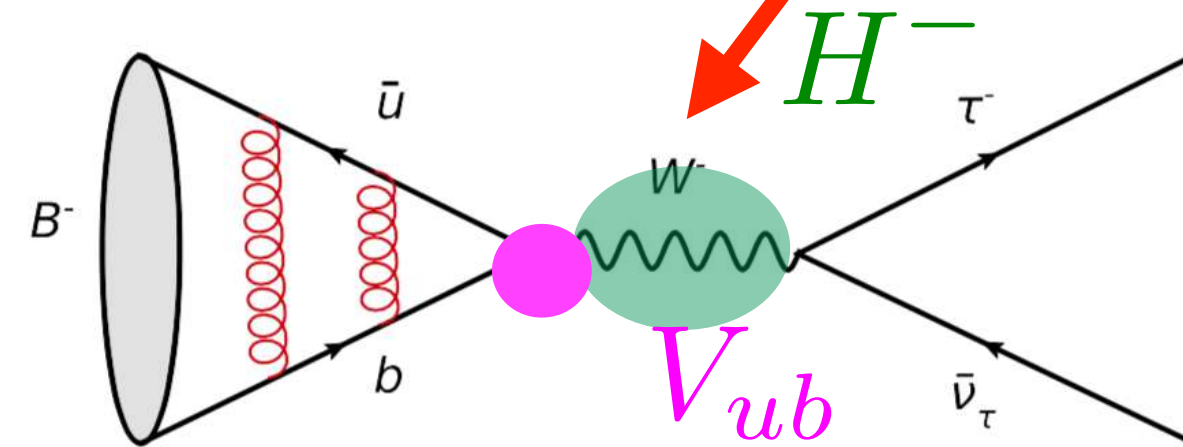
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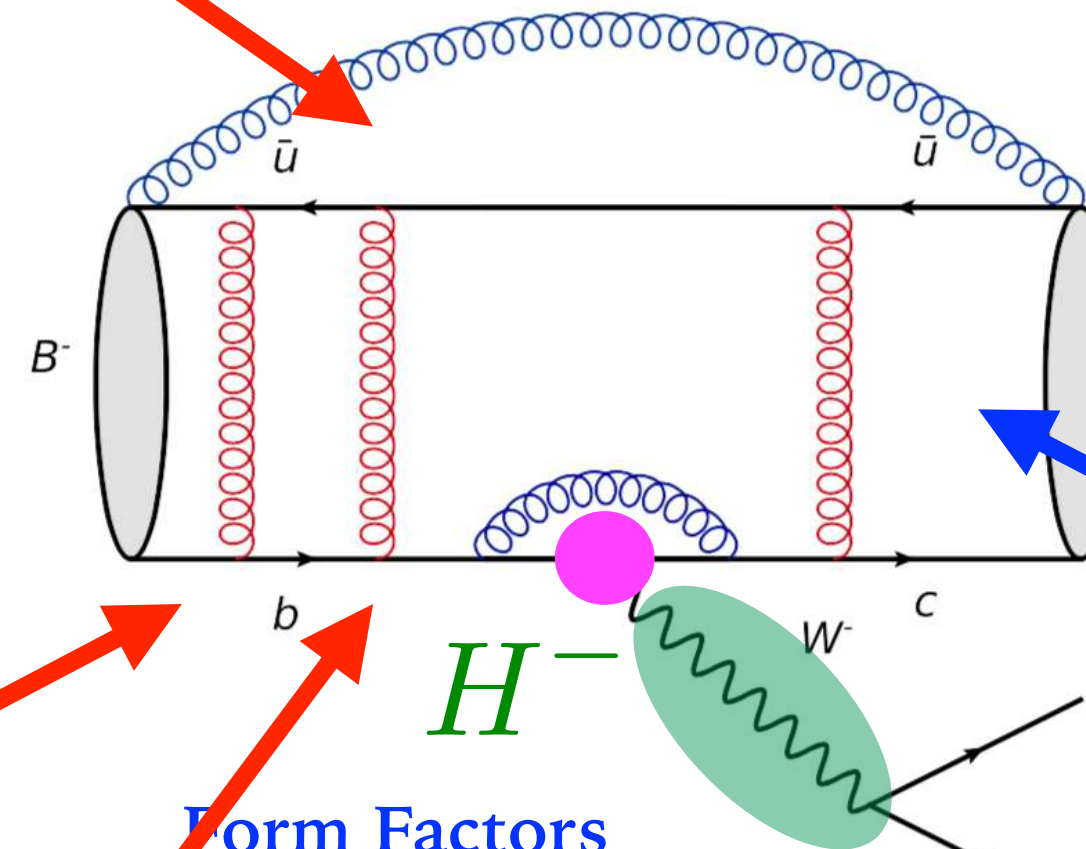
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$b \rightarrow sll$ anomalies
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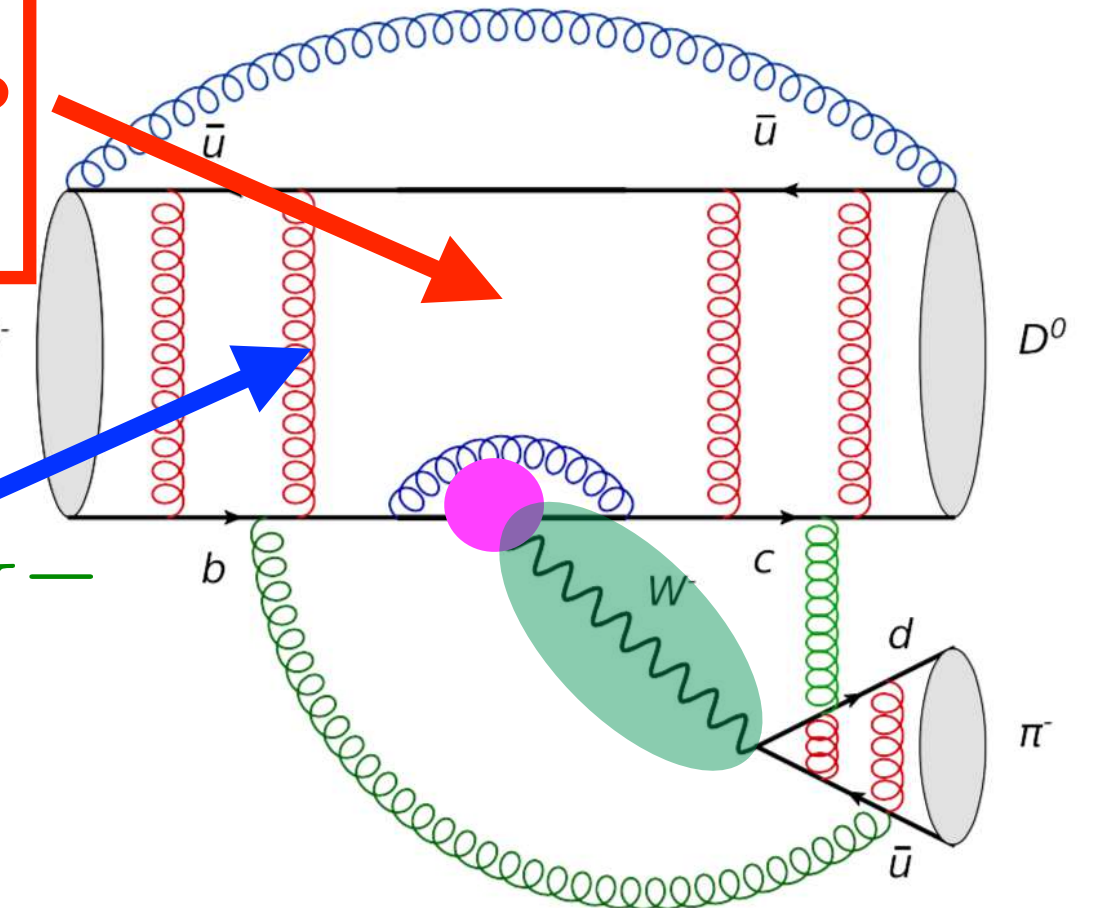
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QCdf

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V_{cb} : inclusive vs. exclusive

$$|V_{cb}|^{\text{incl.,2022}} = (42.16 \pm 0.51) \cdot 10^{-3}$$

Bordone, Caddevilla, Gambino 2107.00604

$$|V_{cb}|^{\text{excl.,PDG}} = (39.5 \pm 0.9) \cdot 10^{-3}.$$

Based on NNNLO-QCD!!!

Fael, Schönwald, Steinhauser 2011.13654

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$$|V_{cb}|^{\text{excl.}} = \left\{ \begin{array}{lll} (38.40 \pm 0.74) \cdot 10^{-3} & \text{FNAL/MILC} & B \rightarrow D^* \ell \nu, \\ (40.3 \pm 0.8) \cdot 10^{-3} & \text{LCSR2 and lattice} & B \rightarrow D^{(*)} \ell \nu, \\ (40.3 \pm 1.7) \cdot 10^{-3} & \text{LCSR1, BaBar} & B \rightarrow D \ell \nu, \\ (41.0 \pm 1.3) \cdot 10^{-3} & \text{LCSR1, Belle} & B \rightarrow D \ell \nu, \\ (41.0 \pm 1.2) \cdot 10^{-3} & \text{lattice + unitarity} & B \rightarrow D \ell \nu, \\ (42.2 \pm 2.3) \cdot 10^{-3} & \text{HPQCD} & B_s \rightarrow D_s^* \ell \nu. \end{array} \right.$$

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Study quark mass definitions

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Improved form factors

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Fael, Schönwald, Steinhauser 2011.13654

$$\Delta M_s^{\text{SM}} = 18.3_{-1.2}^{+0.7} \text{ ps}^{-1}$$

Perfect match

$$\Delta M_s^{\text{SM}} = 16.0_{-1.0}^{+0.6} \text{ ps}^{-1}$$

around 3σ deviation

$$\Delta M_s^{\text{Exp}} = 17.741(20) \text{ ps}^{-1}$$

The D0 dimuon anomaly is still not settled: 3.6σ

The New York Times

A New Clue to Explain Existence

By DENNIS OVERBYE MAY 17, 2010

Physicists at the [Fermi National Accelerator Laboratory](#) are reporting that they have discovered a new clue that could help unravel one of the biggest mysteries of cosmology: why the universe is composed of matter and not its evil-twin opposite, antimatter. If confirmed, the finding portends fundamental discoveries at the new [Large Hadron Collider](#) outside Geneva, as well as a possible explanation for our own existence.

$$A^{\text{Di-muon}} = C_s a_{sl}^s + C_d a_{sl}^d + \frac{1}{2} C_\Delta \Delta \Gamma_d$$

Experiment disagrees with the Standard Model predictions by 4σ

Evidence for an anomalous like-sign dimuon charge asymmetry

[V.M. Abazov et al \(D0 Collaboration\)](#)
Phys. Rev. Lett 105 (2010) 081801

Measurement of the anomalous like-sign dimuon charge asymmetry

[V.M. Abazov et al \(D0 Collaboration\)](#)
Phys. Rev. D 84 (2011) 052007

Study of CP violating charge asymmetry...

[V.M. Abazov et al \(D0 Collaboration\)](#)
Phys. Rev. D 89 (2014) 012002

Theoretical update of Bs mixing

[Alexander Lenz, Uli Nierste](#)
JHEP 0706(2007)072; hep-ph/0612167

Numerical update of lifetimes and mixing parameters

[Alexander Lenz, Uli Nierste](#)
hep-ph/1102.4274

CP violation in the Bs system

[Marina Artuso, Guennadi Borissoy, Alexander Lenz](#)
Rev.Mod.Phys. 88 (2016) no.4,045002

New interpretation of experimental measurement

Understanding the anomalous like-sign dimuon charge asymmetry

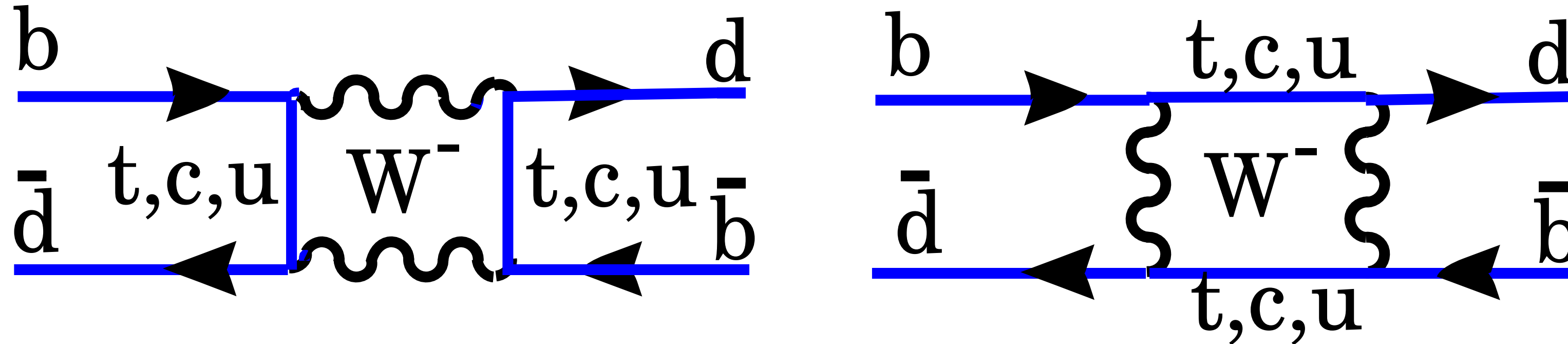
[Guennadi Borissoy, Boris Hoeneisen](#)
Phys. Rev. D 87 (2013) 074020

Effect of Delta Gamma_d on the dimuon asymmetry

[Uli Nierste](#)
Talk at CKM 2014

Mixing

$$\begin{aligned} |B_{q,L}\rangle &= p|B_q\rangle + q|\bar{B}_q\rangle \\ |B_{q,H}\rangle &= p|B_q\rangle - q|\bar{B}_q\rangle \end{aligned}$$



$|M_{12}|$, $|\Gamma_{12}|$ and $\phi = \arg(-M_{12}/\Gamma_{12})$ can be related to three observables:

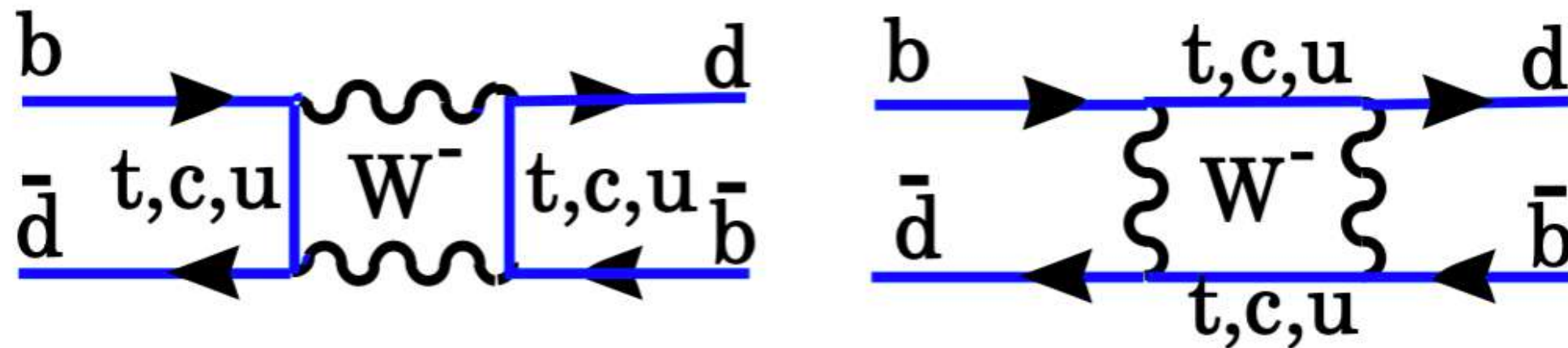
- **Mass difference:** $\Delta M := M_H - M_L \approx 2|M_{12}|$ (off-shell)
 $|M_{12}|$: heavy internal particles: t , SUSY, ...
- **Decay rate difference:** $\Delta\Gamma := \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}| \cos \phi$ (on-shell)
 $|\Gamma_{12}|$: light internal particles: u , c , ... (almost) no NP!!!
- **Flavor specific/semi-leptonic CP asymmetries:** e.g. $B_q \rightarrow X l \nu$ (semi-leptonic)

$$a_{sl} \equiv a_{fs} = \frac{\Gamma(\bar{B}_q(t) \rightarrow f) - \Gamma(B_q(t) \rightarrow \bar{f})}{\Gamma(\bar{B}_q(t) \rightarrow f) + \Gamma(B_q(t) \rightarrow \bar{f})} = \left| \frac{\Gamma_{12}}{M_{12}} \right| \sin \phi$$

Status Quo: Mixing



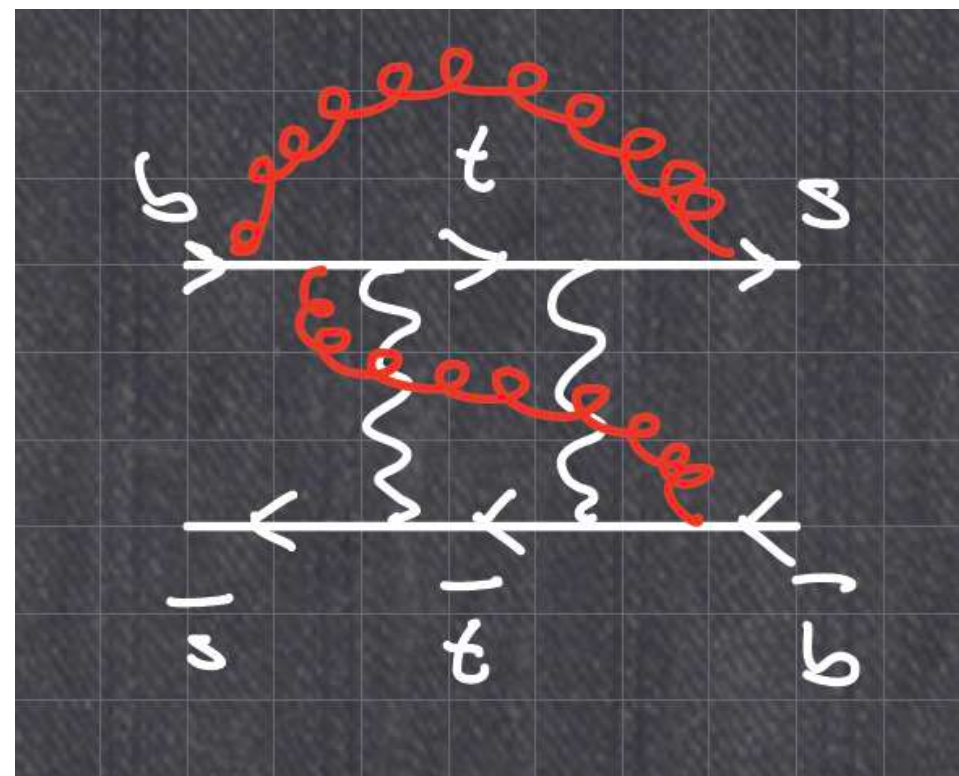
$$\Delta M_s = 2 |M_{12}^s|$$



$$M_{12}^q = \frac{G_F^2}{12\pi^2} \lambda_t^2 M_W^2 S_0(x_t) B f_{B_q}^2 M_{B_q} \hat{\eta}_B,$$

Significant CKM dependence

By far dominant uncertainty

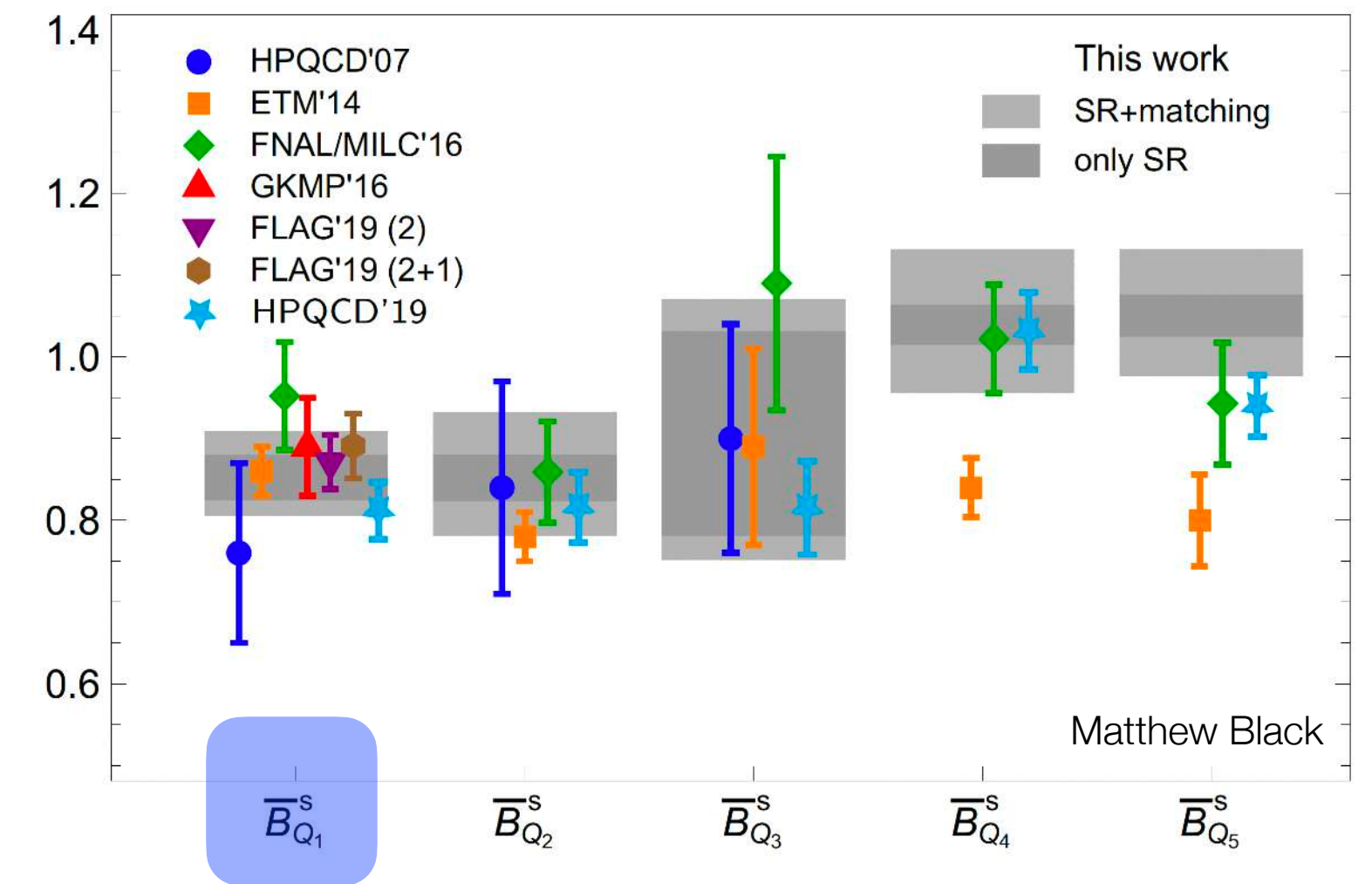


2-loop: Buras, Jamin, Weisz

3-loop: Gorbahn,...

$$Q = \bar{s}^\alpha \gamma_\mu (1 - \gamma_5) b^\alpha \times \bar{s}^\beta \gamma^\mu (1 - \gamma_5) b^\beta$$

$$\langle Q \rangle \equiv \langle B_s^0 | Q | \bar{B}_s^0 \rangle = \frac{8}{3} M_{B_s}^2 f_{B_s}^2 B(\mu)$$



Lattice

- * B_s , B_d and D mixing: [FNAL/MILC 1602.03560](#)
- * Ratio of B_s and B_d mixing: [RBC/UK QCD 1812.08791](#)
- * B_s and B_d mixing: [HQCD 19007.01025](#)

HQET-sum rules: 3-loop + part of NNLO matching:

* B_d mixing:

[Siegen: Grozin, Klein, Mannel, Pivovarov 1606.06054, 1706.05910, 1806.00253](#)

* B_d and D mixing, D^0 , D^+ , B_d and B^+ lifetimes

[Durham: Kirk \(Rome\), AL, Rauh \(Bern\) 1711.02100](#)

* B_s mixing

[Durham: King, AL, Rauh \(Bern\) 1904.00940](#)

* B_s and D_s^+ lifetimes

[Siegen: King \(Durham\), AL, Rauh \(Bern\) 2112.03691](#)

Status Quo: Mixing



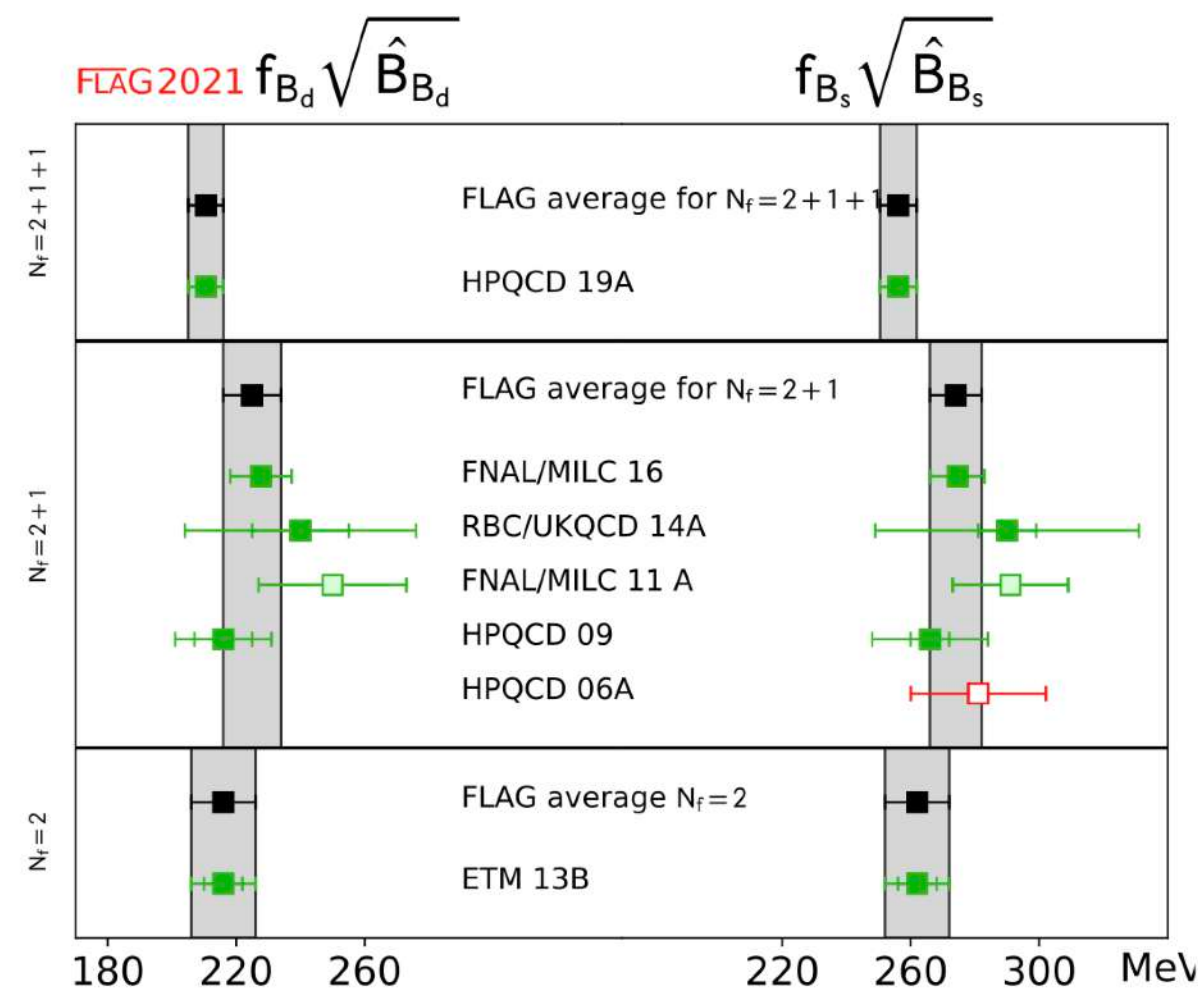
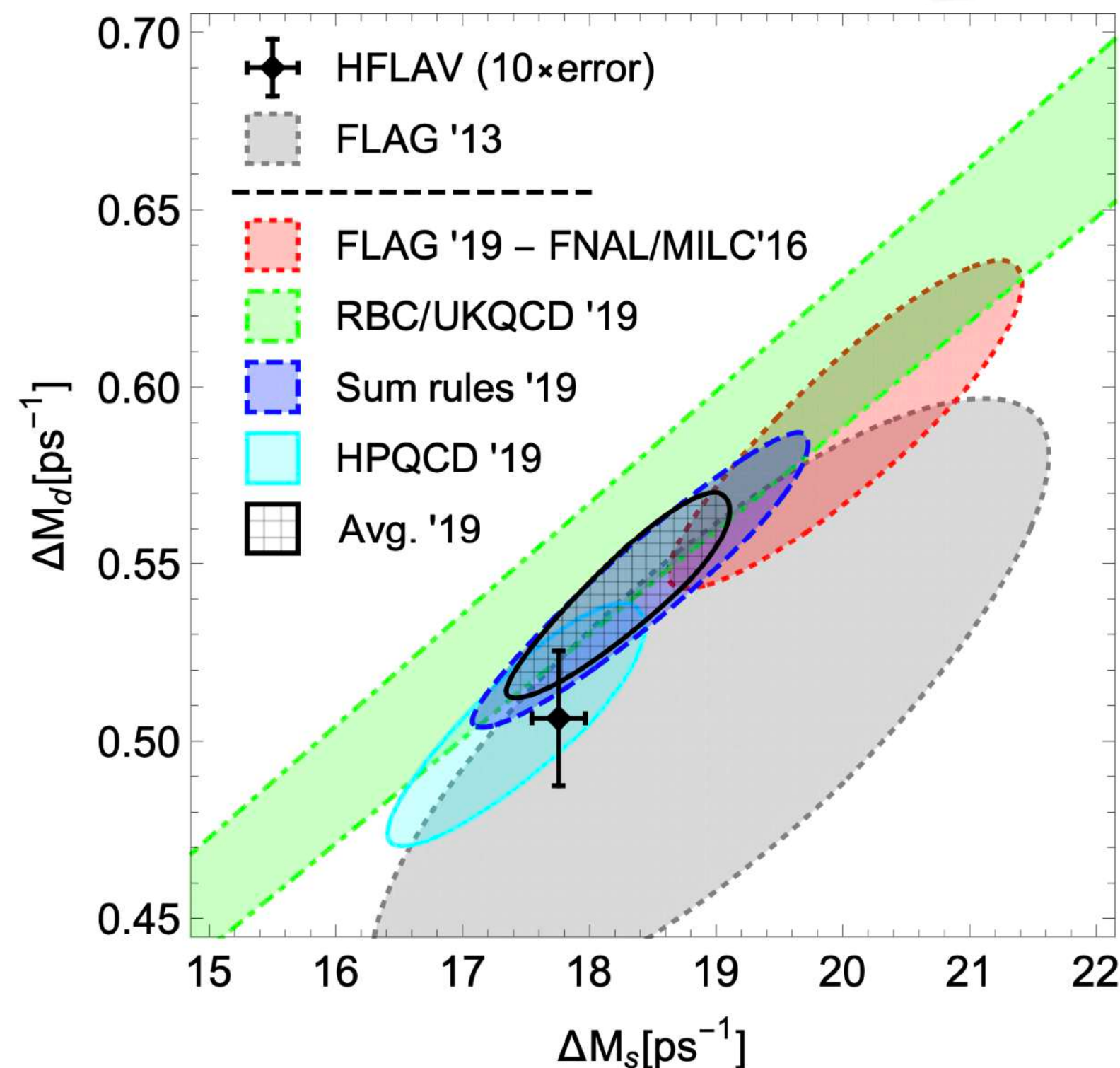
<http://lhcb-public.web.cern.ch>

$$\Delta M_d = (0.5065 \pm 0.0019) \text{ ps}^{-1} \quad \Delta M_d = (0.533^{+0.022}_{-0.036}) \text{ ps}^{-1}$$

$$\Delta M_s = (17.741 \pm 0.020) \text{ ps}^{-1} \quad \Delta M_s = (18.4^{+0.7}_{-1.2}) \text{ ps}^{-1}$$

HFLAV 2021

1909.11087
Average lattice & sum rules



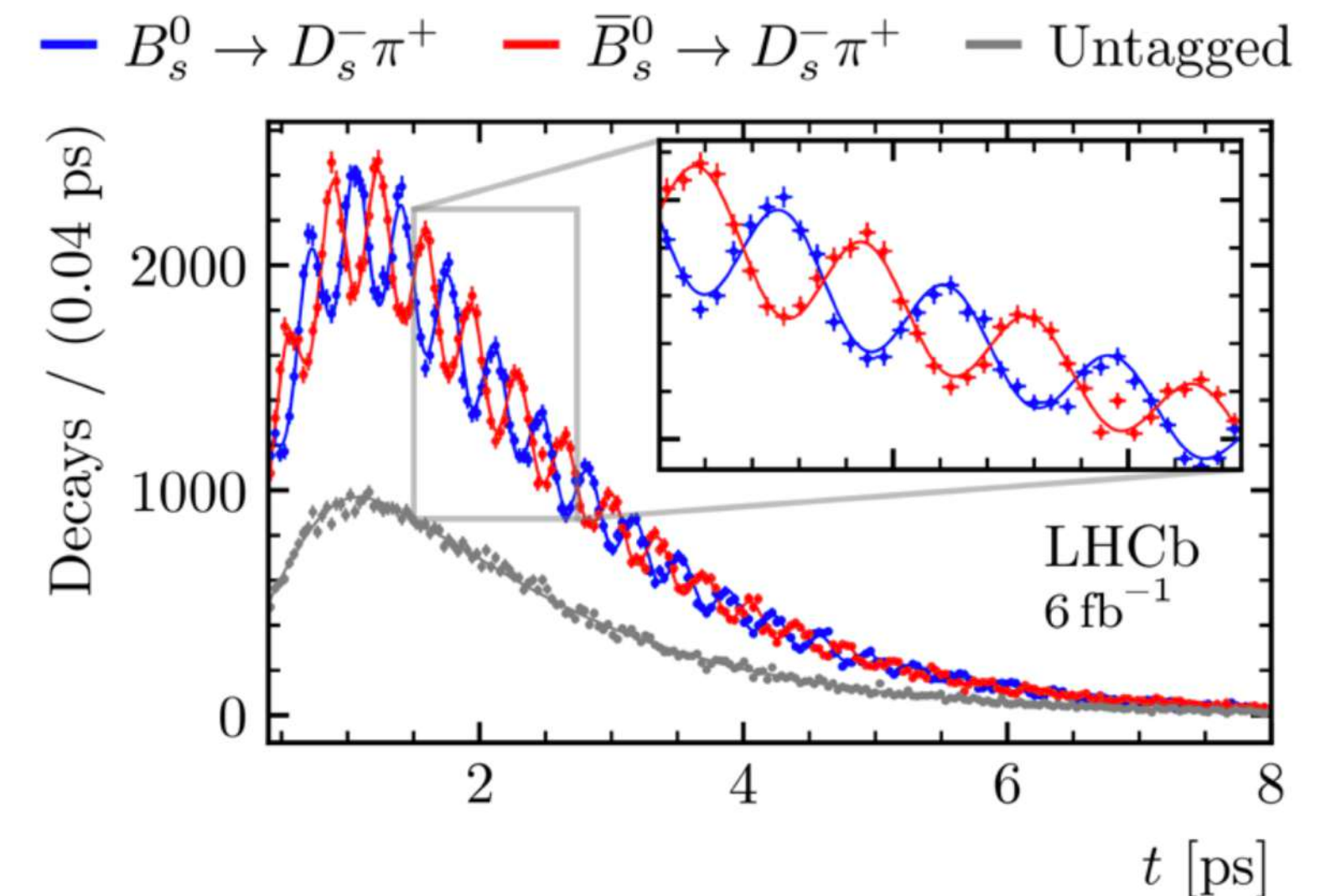
Work in progress by
RBC/UKQCD+JLQCD 2111.11287

12 April 2021: Fascinating quantum mechanics.

Precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency.

"A phenomenon in which quantum mechanics gives a most remarkable prediction" - Richard Feynman

Today, the LHCb Collaboration submitted a paper for publication that reports a precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency. This result is presented also today at the joint [annual conference](#) of the UK Institute of Physics (IOP), organized by the University of Edinburgh. The $B_s^0 - \bar{B}_s^0$ oscillation is a spectacular and fascinating feature of quantum mechanics. The strange beauty particle B_s^0 composed of a [beauty](#) antiquark ($\bar{b}$) bound with a [strange](#) quark s turns into its antiparticle partner $\bar{B}_s^0$ composed of a b quark and an s antiquark ($\bar{s}$) about 3 million million times per second (3×10^{12}) as seen in the image below.



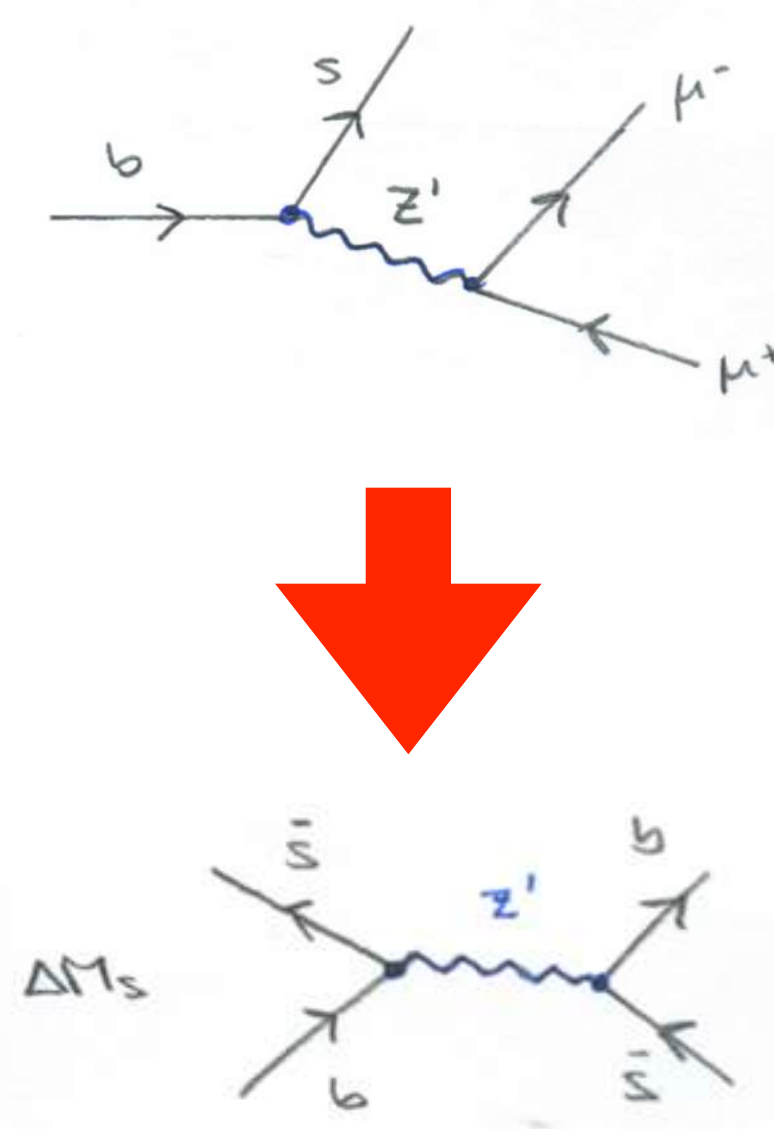
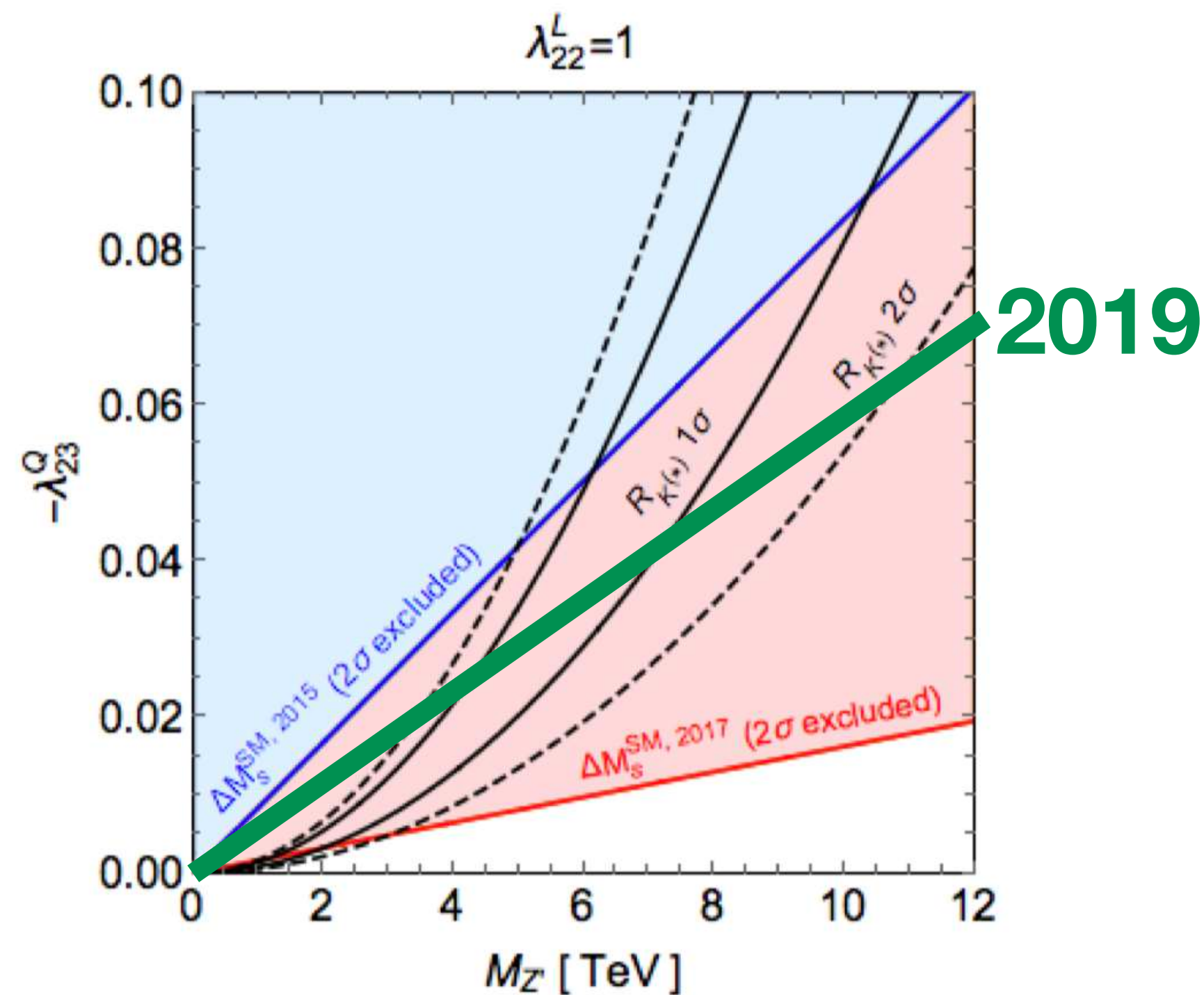
Higher precision for Bag

Status Quo: Mixing

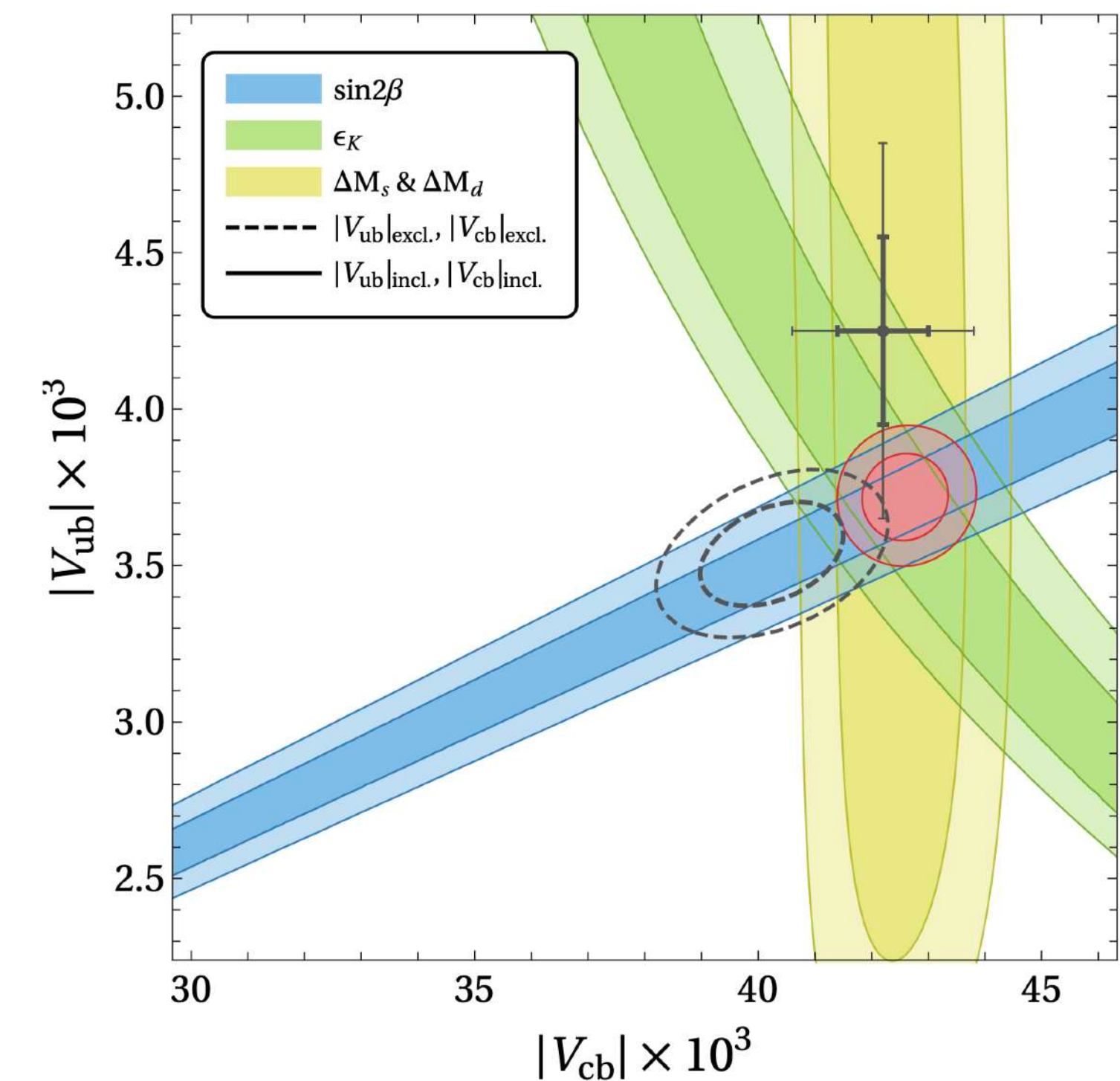


The 2016 theory value for B-mixing has dramatic consequences for BSM models explaining the B anomalies

Direct determination of $V_{td}V_{tb}$, $V_{ts}V_{tb}$ and V_{ts}/V_{td}



Loopy determination of V_{cb} and V_{ub}



One constraint to kill them all?

Luca Di Luzio,^{1,*} Matthew Kirk,^{1,†} and Alexander Lenz^{1,‡}

1712.06572

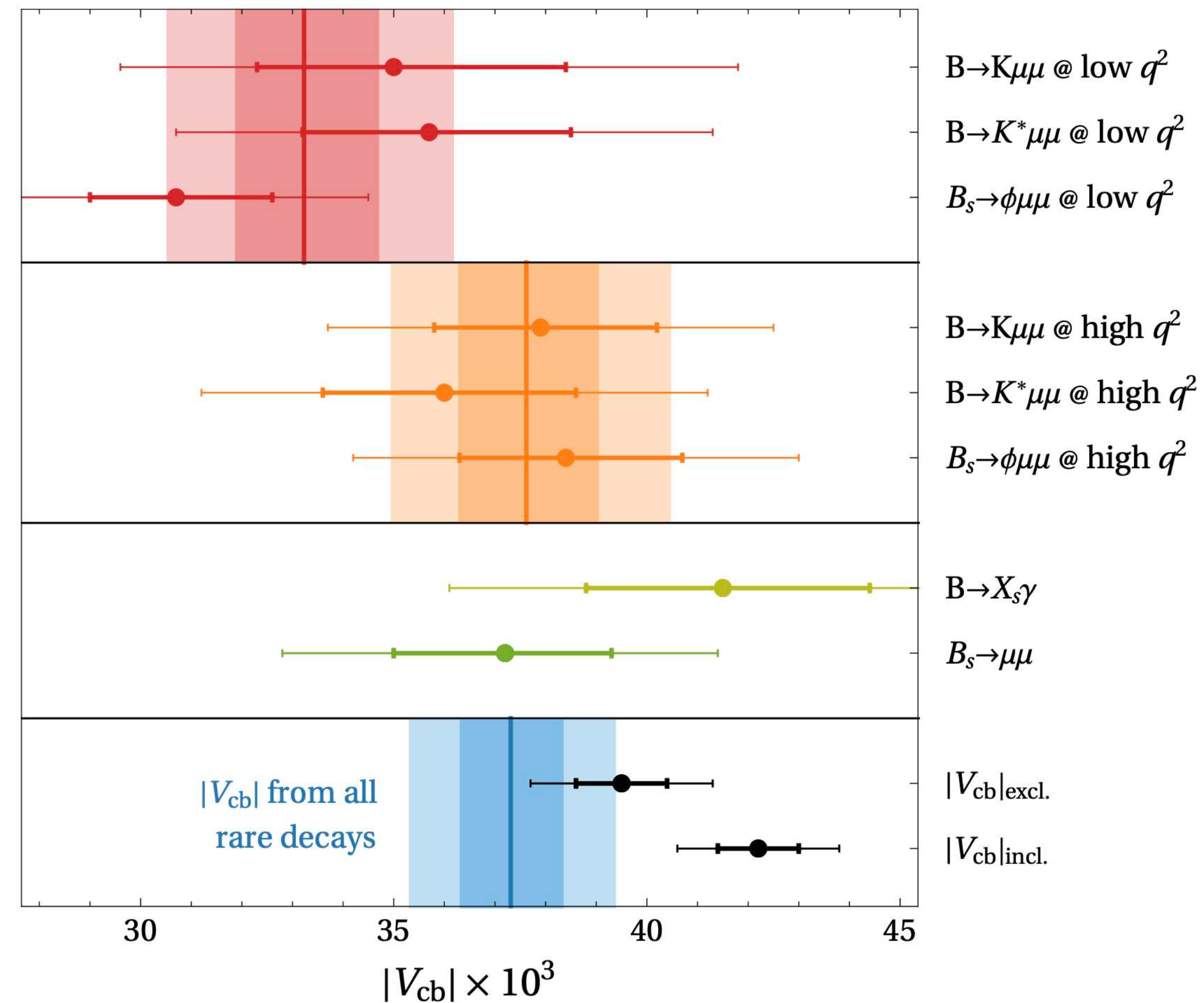
Altmannshofer, Lewis 2112.03437

King, Kirk, AL, Rauh 1911.07856

Old anomalies



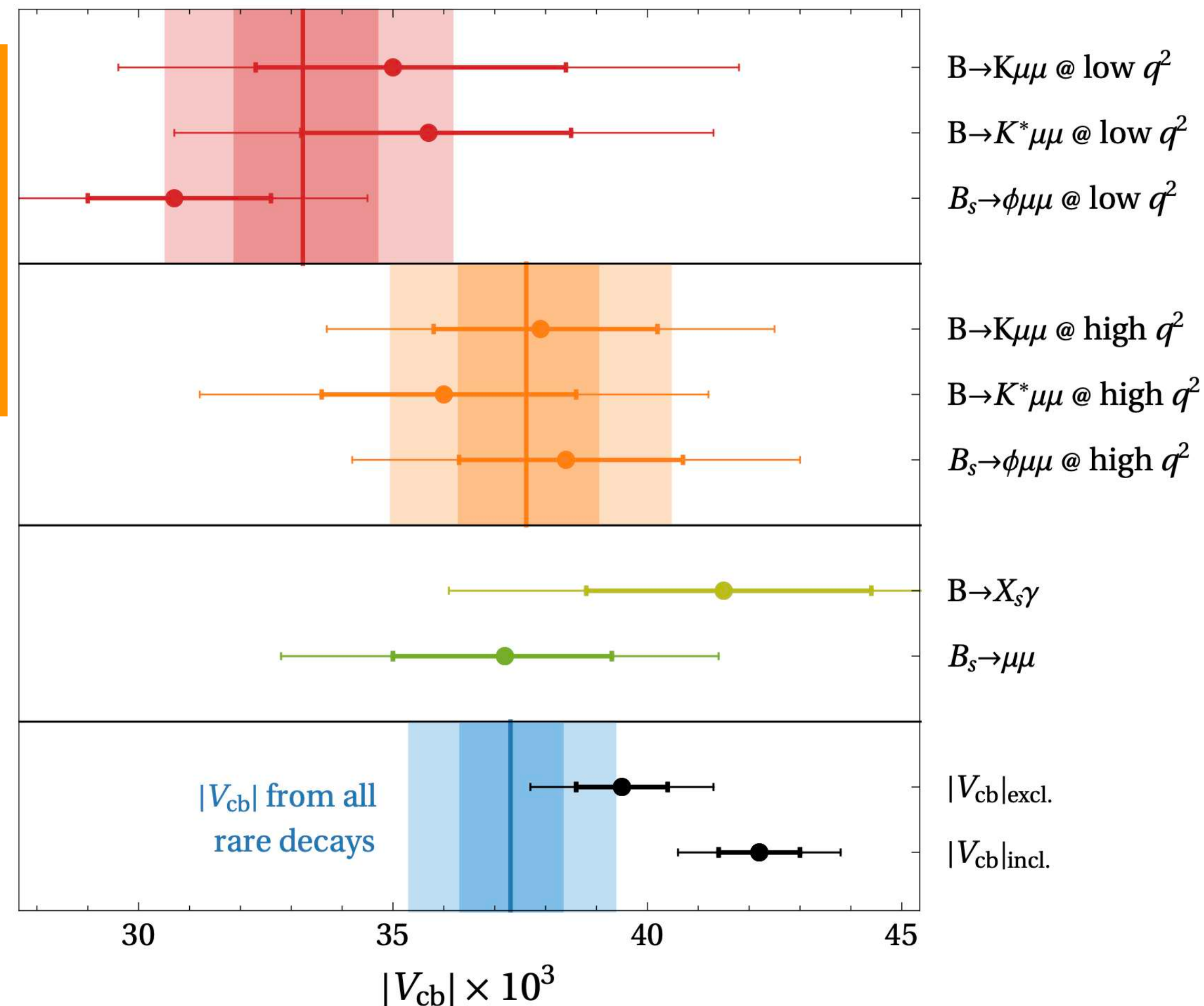
V_{cb} : inclusive vs. exclusive affects also the $b \rightarrow sll$ anomalies



V_{cb} : inclusive vs. exclusive affects also some of the $b \rightarrow sll$ anomalies

**Interesting suggestion
to determine
inclusive B decays
directly with Lattice-QCD**

- [42] S. Hashimoto, *Inclusive semi-leptonic B meson decay structure functions from lattice QCD*, [PTEP 2017 \(2017\) 053B03](#), [arXiv:1703.01881](#).
- [43] M. Hansen, A. Lupo, and N. Tantalo, *Extraction of spectral densities from lattice correlators*, [Phys. Rev. D 99 \(2019\) 094508](#), [arXiv:1903.06476](#).
- [44] J. Bulava and M. T. Hansen, *Scattering amplitudes from finite-volume spectral functions*, [Phys. Rev. D 100 \(2019\) 034521](#), [arXiv:1903.11735](#).
- [45] P. Gambino and S. Hashimoto, *Inclusive Semileptonic Decays from Lattice QCD*, [Phys. Rev. Lett. 125 \(2020\) 032001](#), [arXiv:2005.13730](#).
- [46] J. Bulava et al., *Inclusive rates from smeared spectral densities in the two-dimensional O(3) non-linear σ -model*, [arXiv:2111.12774](#).
- [47] P. Gambino et al., *Lattice QCD study of inclusive semileptonic decays of heavy mesons*, [arXiv:2203.11762](#).



1. **CP violation in Mixing**: Consider a **flavour specific** ($\mathcal{A}_{\bar{f}} = 0 = \bar{\mathcal{A}}_f$) **decay** $B \rightarrow f$

$$A_{\text{fs}}^q = \frac{\Gamma(\bar{B}_q(t) \rightarrow f) - \Gamma(B_q(t) \rightarrow \bar{f})}{\Gamma(\bar{B}_q(t) \rightarrow f) + \Gamma(B_q(t) \rightarrow \bar{f})} \quad \boxed{\bar{\mathcal{A}}_{\bar{f}} = \mathcal{A}_f} = \text{No direct CP violation}$$

$$a_{\text{fs}}^q \approx \frac{|\Gamma_{12}^q|}{|M_{12}^q|} \sin \phi_{12}^q$$

e.g. $B \rightarrow X l \nu$
or $\bar{B}_s \rightarrow D_s^+ \pi^-$
or $\bar{B}_d \rightarrow D^+ K^-$

2. **CP violation in interference of mixing and decay**

$$A_{\text{ind}}^q = \frac{\Gamma(\bar{B}_q(t) \rightarrow f) - \Gamma(B_q(t) \rightarrow f)}{\Gamma(\bar{B}_q(t) \rightarrow f) + \Gamma(B_q(t) \rightarrow f)}$$

e.g. $B_s \rightarrow J/\Psi \phi$
or $B_d \rightarrow J/\Psi K_s$

See also
1511.09466,
hep-ph/0201071

3. **CP violation in decay**

$$A_{\text{dir}}^q = \frac{\Gamma(\bar{B}_q(t) \rightarrow \bar{f}) - \Gamma(B_q(t) \rightarrow f)}{\Gamma(\bar{B}_q(t) \rightarrow \bar{f}) + \Gamma(B_q(t) \rightarrow f)} = \frac{|\bar{\mathcal{A}}_{\bar{f}}|^2 - |\mathcal{A}_f|^2}{|\bar{\mathcal{A}}_{\bar{f}}|^2 + |\mathcal{A}_f|^2}$$

e.g. ΔA_{CP}
or $D^0 \rightarrow \pi^- \pi^+, K^- K^+$

Time evolution of neutral B mesons (quantum mechanics on a macroscopic scale)

$$\Gamma [\bar{B}_q(t) \rightarrow f] = N_f |\mathcal{A}_f|^2 \frac{(1 + |\lambda_f|^2)}{2} (1 + a_{fs}^q) e^{-\Gamma_q t} \left\{ \cosh \left(\frac{\Delta\Gamma_q t}{2} \right) - \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos(\Delta M_q t) - \frac{2 \operatorname{Re}(\lambda_f)}{1 + |\lambda_f|^2} \sinh \left(\frac{\Delta\Gamma_q t}{2} \right) + \frac{2 \operatorname{Im}(\lambda_f)}{1 + |\lambda_f|^2} \sin(\Delta M_q t) \right\},$$

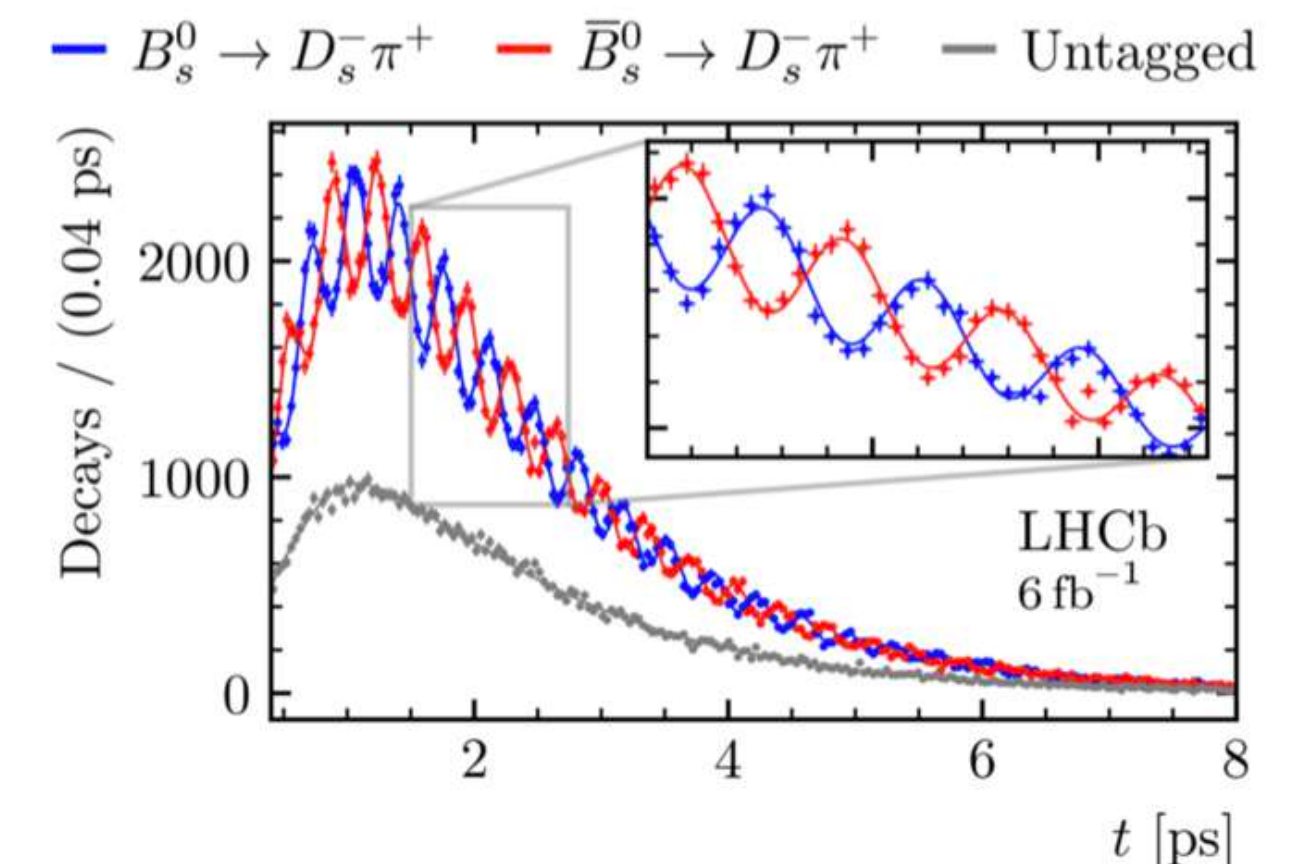
With

$$\mathcal{A}_f = \langle f | \mathcal{H}_{\text{eff}} | B_q \rangle,$$

$$\bar{\mathcal{A}}_f = \langle f | \mathcal{H}_{\text{eff}} | \bar{B}_q \rangle,$$

$$\lambda_f = \frac{q}{p} \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f}$$

and the tiny quantity a_{fs}^q to be defined below



Status Quo: Mixing



$$\Gamma_{12} = \frac{\Lambda^3}{m_b^3} \tilde{\Gamma}_6 \langle \tilde{Q}_6 \rangle + \frac{\Lambda^4}{m_b^4} \tilde{\Gamma}_7 \langle \tilde{Q}_7 \rangle + \dots$$

with $\langle \tilde{Q}_6 \rangle \propto f_B^2 B_{1,2,3}$ and $\langle \tilde{Q}_7 \rangle \propto f_B^2 R_{0,2,3}, m_s/m_b f_B^2 B_{4,5}$ and $\tilde{\Gamma}_i = \tilde{\Gamma}_i^{(0)} + \frac{\alpha}{4\pi} \tilde{\Gamma}_i^{(1)} + \dots$

 $\tilde{\Gamma}_6^{(1)}$

- 1998 Beneke, Buchalla, Greub, AL, Nierste
- 2003 Franco, Lubicz, Mescia, Tarantino
- 2003 Beneke, Buchalla, AL, Nierste
- 2006 AL, Nierste

 $\langle \tilde{Q}_6 \rangle$

- B_1 the same as for ΔM , $B_{2,3,4,5}$ new
- 2016 FNAL/MILC
- 2016-18 Grozin, Klein, Mannel, Pivovarov B_d
- 2017 Kirk, AL, Rauh B_d
- 2019 King, AL, Rauh B_s
- 2019 HPQCD 19007.01025

 $\tilde{\Gamma}_6^{(2)}$

- 2017 partly: Asatrian, Hovhannisyan, Nierste, Yeghiazaryan
- 2020 partly: Asatrian, Asatryan, Hovhannisyan, Nierste, Tumasyan
- 2021 partly: Gerlach, Nierste, Shtabovenko, Steinhauser

 $\langle \tilde{Q}_7 \rangle$

- So far only Vacuum insertion approximation
- 2019 HPQCD 1910.00970

 $\tilde{\Gamma}_7^{(0)}$

- 1996 Beneke, Buchalla, Dunietz
- 2001 Dighe, Hurth, Kim

 $\tilde{\Gamma}_7^{(1)}$

- 202x Nierste and friends

 $\tilde{\Gamma}_8^{(0)}$

- 2007 Badin, Gabbiani, Petrov

$$R_2 = \frac{1}{m_b^2} (\bar{b}^\alpha \overleftarrow{D}_\rho \gamma^\mu (1 - \gamma^5) D^\rho s^\alpha) (\bar{b}^\beta \gamma_\mu (1 - \gamma^5) s^\beta)$$

$$R_3 = \frac{1}{m_b^2} (\bar{b}^\alpha \overleftarrow{D}_\rho (1 - \gamma^5) D^\rho s^\alpha) (\bar{b}^\beta (1 - \gamma^5) s^\beta)$$

This work

$$\Delta\Gamma_s^{HQE} = (0.091 \pm 0.013) \text{ ps}^{-1}$$

$$\Delta\Gamma_d^{HQE} = (2.6 \pm 0.4) \cdot 10^{-3} \text{ ps}^{-1}$$

$$\Delta\Gamma_s^{HFLAV} = (0.082 \pm 0.005) \text{ ps}^{-1}$$

$$\Delta\Gamma_d^{HFLAV} = (-1.3 \pm 6.6) \cdot 10^{-3} \text{ ps}^{-1}$$

1912.07621

HFLAV, ATLAS 1605.07485

Status Quo: Mixing



$$\Gamma_{12} = \frac{\Lambda^3}{m_b^3} \tilde{\Gamma}_6 \langle \tilde{Q}_6 \rangle + \frac{\Lambda^4}{m_b^4} \tilde{\Gamma}_7 \langle \tilde{Q}_7 \rangle + \dots$$

with $\langle \tilde{Q}_6 \rangle \propto f_B^2 B_{1,2,3}$ and $\langle \tilde{Q}_7 \rangle \propto f_B^2 R_{0,2,3}, m_s/m_b f_B^2 B_{4,5}$ and $\tilde{\Gamma}_i = \tilde{\Gamma}_i^{(0)} + \frac{\alpha}{4\pi} \tilde{\Gamma}_i^{(1)} + \dots$

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- 2017 Kirk, AL, Rauh B_d
- 2019 King, AL, Rauh B_s
- 2019 HPQCD 19007.01025

 $\langle \tilde{Q}_7 \rangle$

- So far only Vacuum insertion approximation
- 2019 HPQCD 1910.00970

$$R_2 = \frac{1}{m_b^2} (\bar{b}^\alpha \overleftarrow{D}_\rho \gamma^\mu (1 - \gamma^5) D^\rho s^\alpha) (\bar{b}^\beta \gamma_\mu (1 - \gamma^5) s^\beta)$$

$$R_3 = \frac{1}{m_b^2} (\bar{b}^\alpha \overleftarrow{D}_\rho (1 - \gamma^5) D^\rho s^\alpha) (\bar{b}^\beta (1 - \gamma^5) s^\beta)$$

This work

Higher perturbative orders and determinations of dim. 7 Bag

Status Quo: CPV in Mixing



In the ratio Γ_{12}/M_{12} theory uncertainties are cancelling

$$\text{Re} \left(\frac{\Gamma_{12}^s}{M_{12}^s} \right) = -\frac{\Delta\Gamma_s}{\Delta M_s}, \quad \text{Im} \left(\frac{\Gamma_{12}^s}{M_{12}^s} \right) = a_{fs}^s.$$

$$-\frac{\Gamma_{12}^s}{M_{12}^s} = \frac{\lambda_c^2 \Gamma_{12}^{s,cc} + 2\lambda_c \lambda_u \Gamma_{12}^{s,uc} + \lambda_u^2 \Gamma_{12}^{s,uu}}{\lambda_t^2 \tilde{M}_{12}^s} = \frac{\Gamma_{12}^{s,cc}}{\tilde{M}_{12}^s} + 2 \frac{\lambda_u}{\lambda_t} \frac{\Gamma_{12}^{s,cc} - \Gamma_{12}^{s,uc}}{\tilde{M}_{12}^s} + \left(\frac{\lambda_u}{\lambda_t} \right)^2 \frac{\Gamma_{12}^{s,cc} - 2\Gamma_{12}^{s,uc} + \Gamma_{12}^{s,uu}}{\tilde{M}_{12}^s}$$

- No CKM dependence!
- No GIM suppression!
- No imaginary part!
- Small $\approx \mathcal{O}(5 \cdot 10^{-3})$
- Leading contribution to $\Delta\Gamma$

- CKM suppression
- GIM suppression
- Imaginary part via CKM
- Leading contribution to a_{fs}
- Tiny contribution to $\Delta\Gamma$

$$\frac{V_{ub}V_{ud}}{V_{tb}V_{td}} = \lambda^{0.8}$$

$$\frac{V_{ub}V_{us}}{V_{tb}V_{ts}} = \lambda^{2.8}$$

- Stronger CKM suppression
- Very strong GIM suppression
- Imaginary part via CKM
- Subleading contribution to a_{fs} and $\Delta\Gamma$

$$a_{sl}^{s,\text{Exp}} = (60 \pm 280) \cdot 10^{-5},$$

$$a_{sl}^{d,\text{Exp}} = (-21 \pm 17) \cdot 10^{-4}.$$

$$a_{sl}^{s,\text{SM}} = (2.06 \pm 0.18) \cdot 10^{-5},$$

$$a_{sl}^{d,\text{SM}} = (-4.73 \pm 0.42) \cdot 10^{-4}.$$

HFLAV 1970?

1912.07621

Alternative Scale Setting

ϵ (GeV)	Γ_{12}^s/M_{12}^s	Γ_{12}^d/M_{12}^d
0.	$-0.00499 + 0.000022I$	$-0.00497 - 0.00050I$
0.2.	$-0.00494 + 0.000023I$	$-0.00492 - 0.00053I$
0.5.	$-0.00484 + 0.000026I$	$-0.00482 - 0.00059I$
1.0	$-0.00447 + 0.000037I$	$-0.00448 - 0.00084I$
1.5.	$-0.00287 + 0.000091I$	$-0.00309 - 0.0021I$

Theory uncertainties might be larger, but this will only become relevant if the exp. precision reaches around

$$2 a_{fs}^{\text{SM}}$$

**AL, Piscopo, Vlahos
2007.03022**

CPV in Decay



$$A_{\text{dir.CP},f}(t) = \frac{\Gamma(\bar{B}_s^0(t) \rightarrow \bar{f}) - \Gamma(B_s^0(t) \rightarrow f)}{\Gamma(\bar{B}_s^0(t) \rightarrow \bar{f}) + \Gamma(B_s^0(t) \rightarrow f)} = \frac{|\bar{\mathcal{A}}_{\bar{f}}|^2 - |\mathcal{A}_f|^2}{|\bar{\mathcal{A}}_{\bar{f}}|^2 + |\mathcal{A}_f|^2} = \frac{2|r| \sin(\phi_{\text{Penguin}}^{\text{QCD}} - \phi_{\text{Tree}}^{\text{QCD}}) \sin[\arg(\lambda_u) - \arg(\lambda_c)]}{1 + |r|^2 + 2|r| \cos(\phi_{\text{Penguin}}^{\text{QCD}} - \phi_{\text{Tree}}^{\text{QCD}}) \cos[\arg(\lambda_u) - \arg(\lambda_c)]}$$

$$\mathcal{A}_f = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} + \arg(\lambda_c)]} + |\mathcal{A}_f^{\text{Penguin}}| e^{i[\phi_{\text{Penguin}}^{\text{QCD}} + \arg(\lambda_u)]}$$

$$\bar{\mathcal{A}}_{\bar{f}} = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} - \arg(\lambda_c)]} + |\mathcal{A}_f^{\text{Penguin}}| e^{i[\phi_{\text{Penguin}}^{\text{QCD}} - \arg(\lambda_u)]}$$

The **leading contribution to the CP asymmetry is proportional to** $r = |\mathcal{A}_f^{\text{Penguin}}| / |\mathcal{A}_f^{\text{Tree}}|$

Extremely hard to predict!

(In the case of CPV in interference the leading term was free of hadronic uncertainties and only the penguin corrections depended on r)



Non-leptonic decays

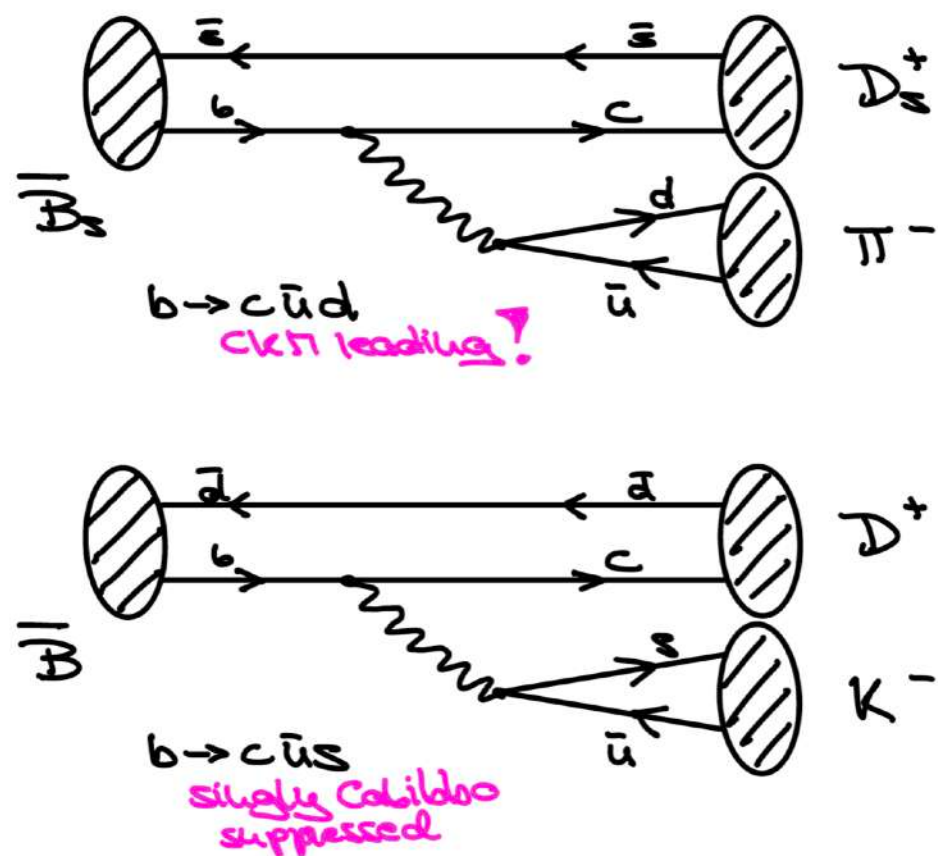


3 σ to 9 σ deviation of experiment from QCDf predictions with standard error estimates

Talk by Daniel Ferlewicz, Nico Gubernari

N. Skidmore

Colour-allowed Tree-level Decays



- CKM leading decays
- There are no annihilation, penguins, ...
- QCDf should work at its best!

Beneke, Buchalla, Neubert, Sachrajda 1999...

$$\langle D_q^{(*)+} L^- | \mathcal{Q}_i | \bar{B}_q^0 \rangle = \sum_j F_j^{\bar{B}_q^0 \rightarrow D_q^{(*)}}(M_L^2) \times \int_0^1 du T_{ij}(u) \phi_L(u) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{m_b}\right)$$

$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)$
(Belle 2111.04978)

$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)$

$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)$

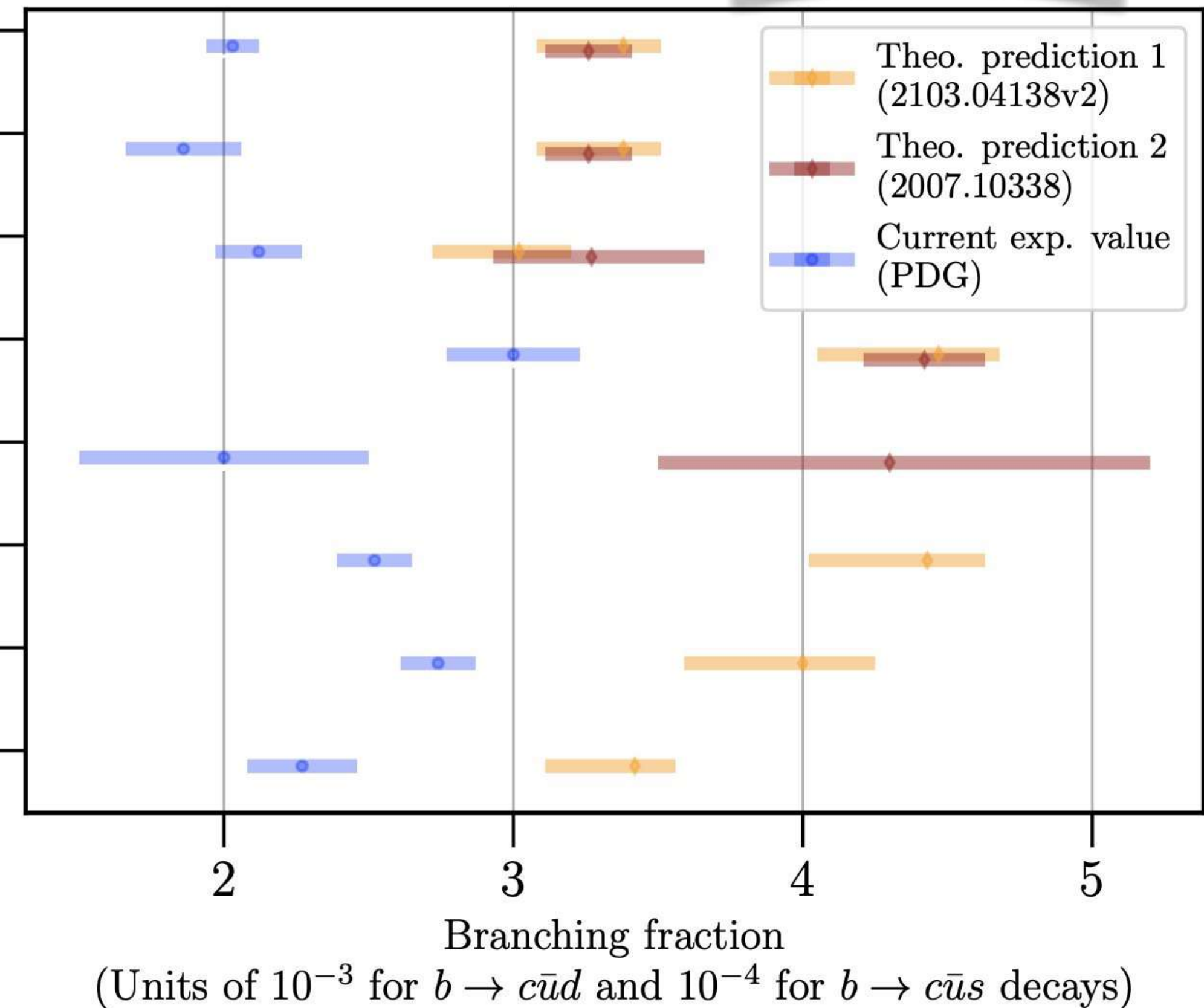
$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^+ \pi^-)$

$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^{*+} \pi^-)$

$\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)$

$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)$

$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^+ K^-)$



Non-leptonic decays

3 σ to 9 σ deviation of experiment from QCDf predictions with standard error estimates



Non-leptonic decays



What could go wrong?

Non-leptonic decays



What could go wrong?



Alexander Lenz

@alexlenz42

...

According to the new Belle measurement in 2111.04978, the decay $\bar{B}_d \rightarrow D^+ K^-$ is around 7 sigma of the QCD factorisation prediction in 2007.10338. Where is this discrepancy rooted?

QCD factorisation

90.9%

New Physics

9.1%

Experiment

0%

33 votes · Final results

9:47 AM · Nov 10, 2021 · Twitter Web App

Non-leptonic decays



What could go wrong?



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- Huber, Kränkl 1606.02888
- Bordone, Gubernari, Huber, Jung, vanDyk 2007.10338
- Iguro, Kitahara 2008.01086
- Cai, Deng, Li, Yang 2103.04138
- Bordone, Greljo, Maryocca 2103.10332
- Beneke, Böer, Finauro, Vos 2107.03819

Similar for $B_s \rightarrow D_s^\mp K^\pm$

- Fleischer, Malami 2110.04240, 2109.04950

Non-leptonic decays



What could go wrong?



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Similar for $B_s \rightarrow D_s^\mp K^\pm$

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In the SM the determination of γ is super precise

The ultimate theoretical error on γ from $B \rightarrow DK$ decays

Joachim Brod^{1,*} and Jure Zupan^{1,†}

¹Department of Physics, University of Cincinnati, Cincinnati, Ohio 45221, USA

Abstract

The angle γ of the standard CKM unitarity triangle can be determined from $B \rightarrow DK$ decays with a very small irreducible theoretical error, which is only due to second-order electroweak corrections. We study these contributions and estimate that their impact on the γ determination is to introduce a shift $|\delta\gamma| \lesssim \mathcal{O}(10^{-7})$, well below any present or planned future experiment.

If there are BSM effects in non-leptonic decays, the determination of γ can be modified by $\mathcal{O}(5^\circ)$

PHYSICAL REVIEW D **92**, 033002 (2015)

New physics effects in tree-level decays and the precision in the determination of the quark mixing angle γ

Joachim Brod

PRISMA Cluster of Excellence and Mainz Institute for Theoretical Physics,
Johannes Gutenberg University, 55099 Mainz, Germany

Alexander Lenz, Gilberto Tetlalmatzi-Xolocotzi, and Martin Wiebusch
Institute for Particle Physics Phenomenology, Department of Physics, Durham University,
South Road, Durham DH1 3LE, United Kingdom

update

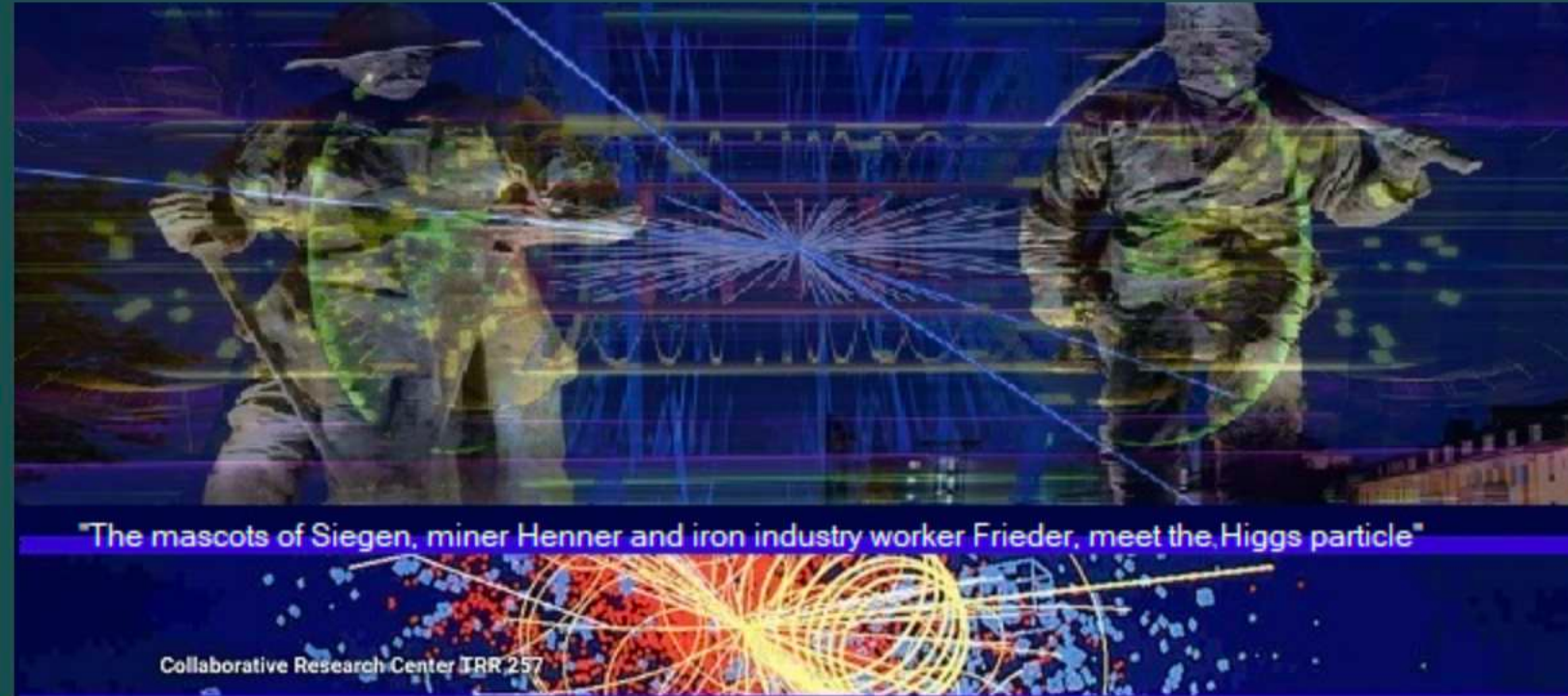
AL, Tetlalmatzi-Xolocotzi
1912.07621

Non-leptonic decays



Things to check

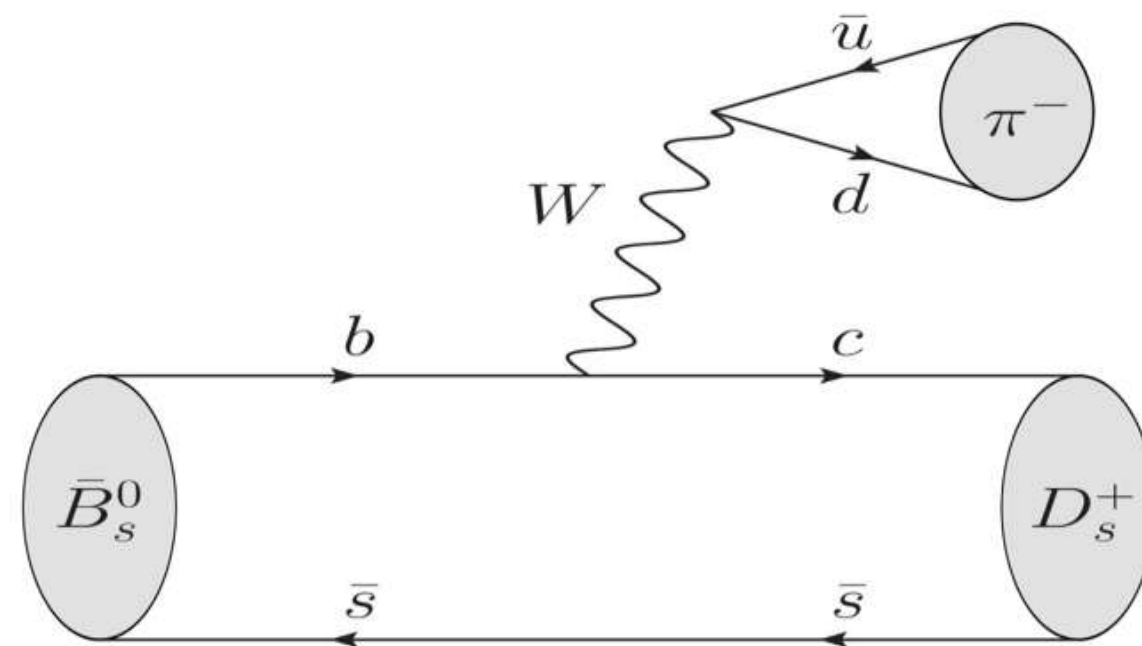
- Reconsidering QCDf uncertainty estimates: **Khodjamirian, Piscopo, Rusov** if new effects will be found, then this might also affect the estimate of charm loops
- **BSM** in $b \rightarrow c\bar{u}d$ would also affect $\tau(B^+)/\tau(B_d)$ **AL, Müller, Piscopo, Rusov**
- Consider CP asymmetries in colour allowed tree-level decays
there is only one amplitude in the SM



Status and prospects of Non-leptonic B meson decays

31 May 2022 to 2 June 2022
Europe/Berlin timezone

The aim of this event is to discuss the current status in theory and experiment of non-leptonic B meson decays. This entails talks on calculation techniques, including QCD factorization and perturbative QCD with special emphasis on the current status of estimating power corrections. Moreover, this workshop will include sessions devoted to the discussion of different puzzles, old and new, arising within the context of purely hadronic B meson processes. Here, discrepancies between the theoretical and the experimental determinations may indicate either potential physics beyond the SM or a critical reassessment of our theory tools. Finally, future experimental prospects on the expected precision and the measurement of different non-leptonic channels will also be addressed.



The University of Siegen has around 18.000 students and it has a large theoretical flavour physics group with around 40 members. Downtown Siegen offers many pubs, restaurants and cafes, but also theaters, cinemas and concert halls.



<https://indico.scc.kit.edu/event/2641/>

Non-leptonic decays



**If you are fed up with our (=theorists)
estimates
of hadronic effects**

Flavour specific decays



- a_{fs}^q is typically measured with semi-leptonic B_q decays

$$a_{sl}^{s,\text{Exp}} = (60 \pm 280) \cdot 10^{-5},$$
$$a_{sl}^{d,\text{Exp}} = (-21 \pm 17) \cdot 10^{-4}.$$

HFLAV 1970?

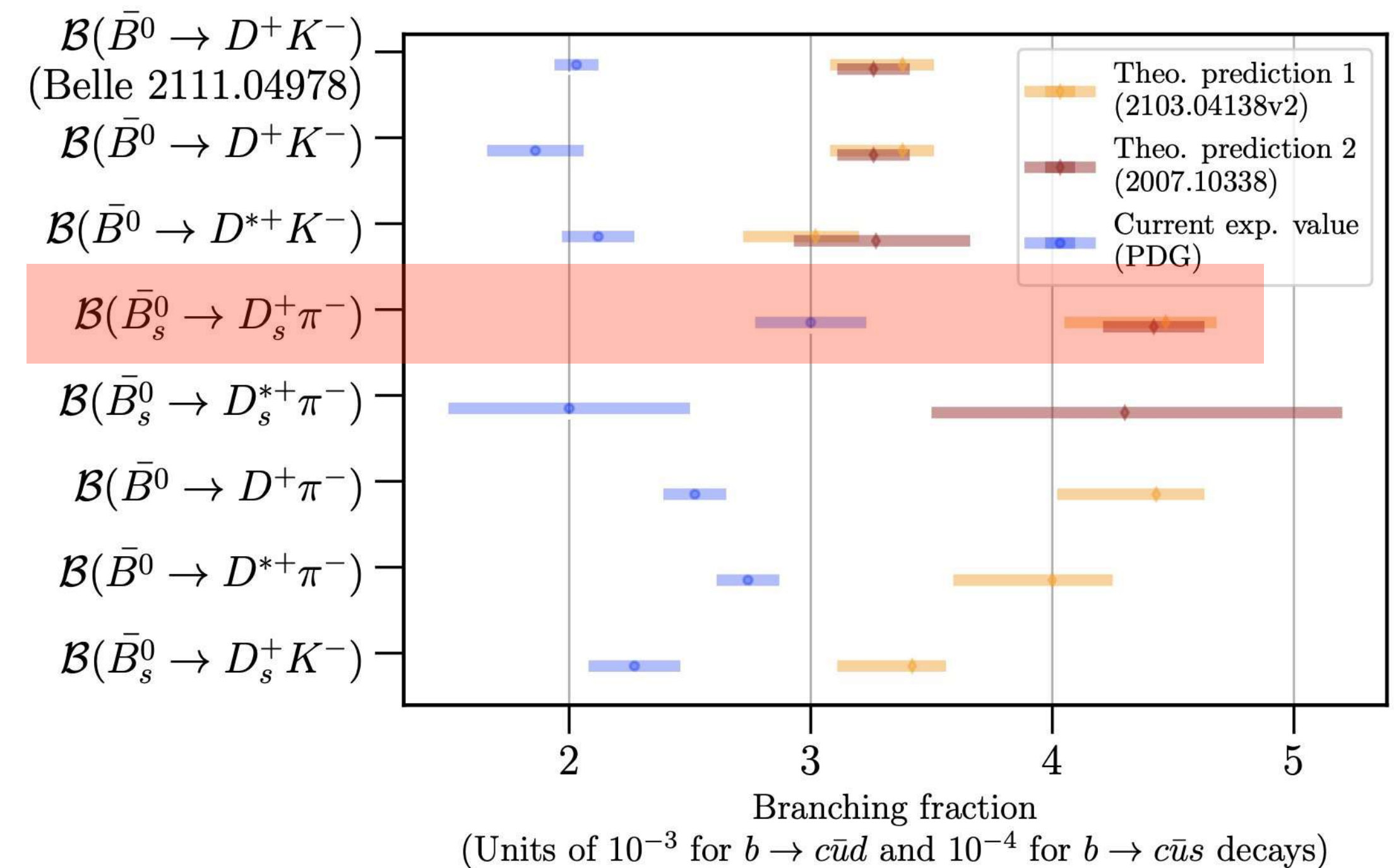
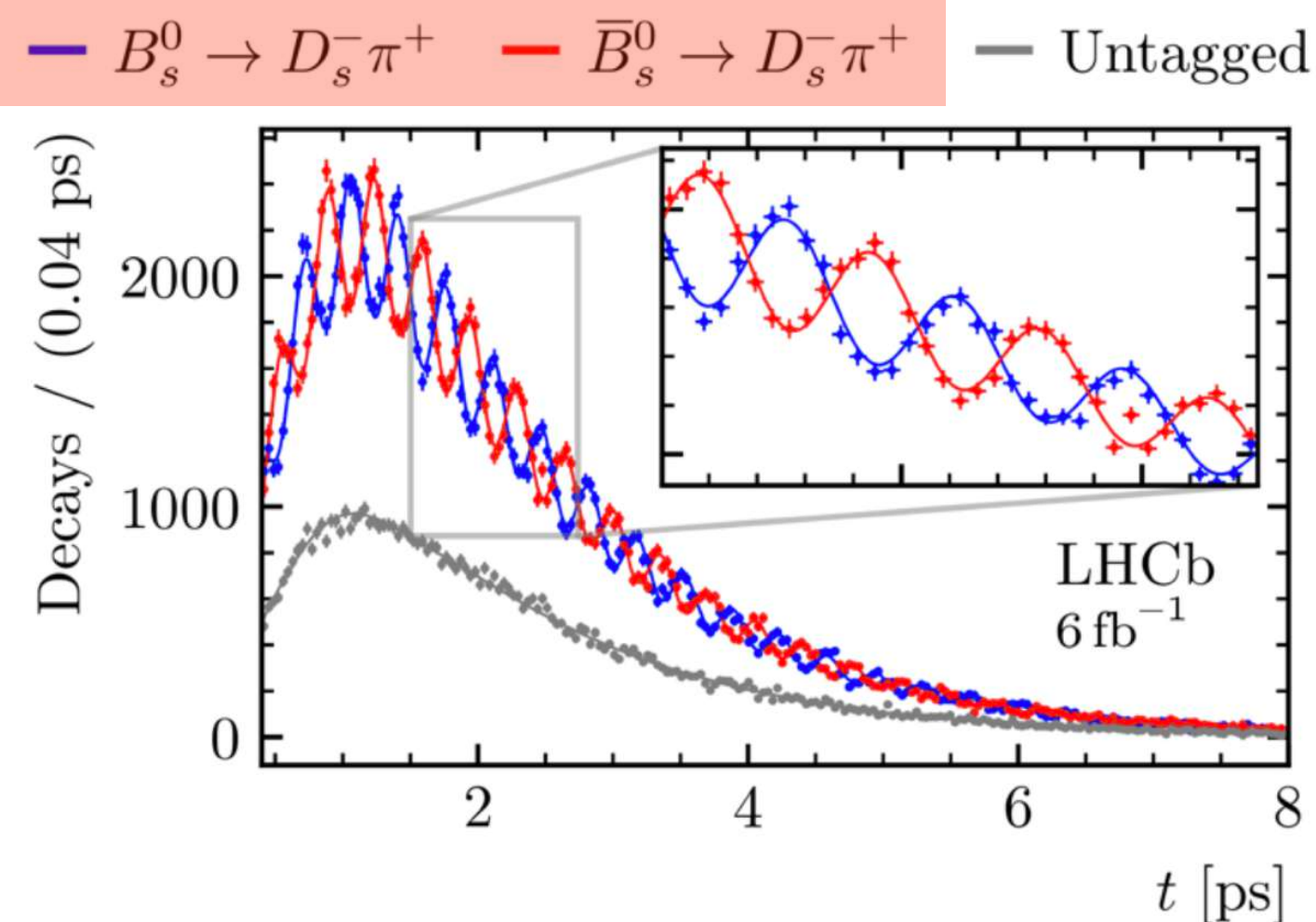
- a_{fs}^q is typically measured with semi-leptonic B_q decays
- One could also use the flavour specific $\bar{B}_s \rightarrow D_s^+ \pi^-$ decay

12 April 2021: Fascinating quantum mechanics.

Precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency.

"A phenomenon in which quantum mechanics gives a most remarkable prediction" - Richard Feynman

Today, the LHCb Collaboration submitted a paper for publication that reports a precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency. This result is presented also today at the joint [annual conference](#) of the UK Institute of Physics (IOP), organized by the University of Edinburgh. The $B_s^0 - \bar{B}_s^0$ oscillation is a spectacular and fascinating feature of quantum mechanics. The strange beauty particle B_s^0 composed of a [beauty](#) antiquark ($\bar{b}$) bound with a [strange](#) quark s turns into its antiparticle partner $\bar{B}_s^0$ composed of a b quark and an s antiquark ($\bar{s}$) about 3 million million times per second (3×10^{12}) as seen in the image below.



Flavour specific decays



- a_{fs}^q is typically measured with semi-leptonic B_q decays
- One could also use the flavour specific $\bar{B}_s \rightarrow D_s^+ \pi^-$ decay
- Assume: there is **new physics** in these decays, potentially CP violating

$$\begin{aligned} \mathcal{A}_f &= |\mathcal{A}_f^{\text{SM}}| e^{i\phi^{\text{SM}}} e^{i\varphi^{\text{SM}}} + |\mathcal{A}_f^{\text{BSM}}| e^{i\phi^{\text{BSM}}} e^{i\varphi^{\text{BSM}}} \\ &=: |\mathcal{A}_f^{\text{SM}}| e^{i\phi^{\text{SM}}} e^{i\varphi^{\text{SM}}} (1 + r e^{i\phi} e^{i\varphi}) , \end{aligned}$$

Discrepancy QCDf vs Exp. suggests $r \approx 0.1 - 0.2$

Flavour specific decays



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- One could also use the flavour specific $\bar{B}_s \rightarrow D_s^+ \pi^-$ decay
- Assume: there is new physics in these decays, potentially CP violating
- Derive CP asymmetry

$$A_{fs}^q = \frac{a_{fs}^q - 2r \sin \phi \sin \varphi + 2a_{fs}^q r \cos \phi \cos \varphi + a_{fs}^q r^2}{1 + 2r \cos \phi \cos \varphi + r^2 - 2a_{fs}^q r \sin \phi \sin \varphi} \approx a_{fs}^q - A_{dir}^q$$

$$\approx 2r \sin \phi \sin \varphi < 0.40$$

Constrained by
semi-leptonic
Measurements

$$a_{sl}^{s,Exp} = (60 \pm 280) \cdot 10^{-5},$$

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HFLAV 1970?

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Gershon, AL, Rusov, Skidmore
2111.04478

$$A_{fs}^q = \frac{a_{fs}^q - 2r \sin \phi \sin \varphi + 2a_{fs}^q r \cos \phi \cos \varphi + a_{fs}^q r^2}{1 + 2r \cos \phi \cos \varphi + r^2 - 2a_{fs}^q r \sin \phi \sin \varphi} \approx a_{fs}^q - A_{dir}^q$$

$$\approx 2r \sin \phi \sin \varphi < 0.40$$

**Significant exp. deviation of A_{fs}^q from a_{sl}^q
= unambiguous and theory independent
signal for BSM**

Constrained by
semi-leptonic
Measurements

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$$a_{sl}^{d,Exp} = (-21 \pm 17) \cdot 10^{-4}.$$

HFLAV 1970?



Quirks in Quark Flavour Physics

The workshop will take place in the beautiful coastal city of Zadar, Croatia.



Jun 14 – 17, 2022
Zadar, Croatia
Europe/Berlin timezone

We will discuss the state of the current anomalies, puzzles, and quirks in quark flavour physics. Participants will contribute in the fields of experimental physics, phenomenology, and lattice field theory.

<https://indico.ph.tum.de/event/6994/>

